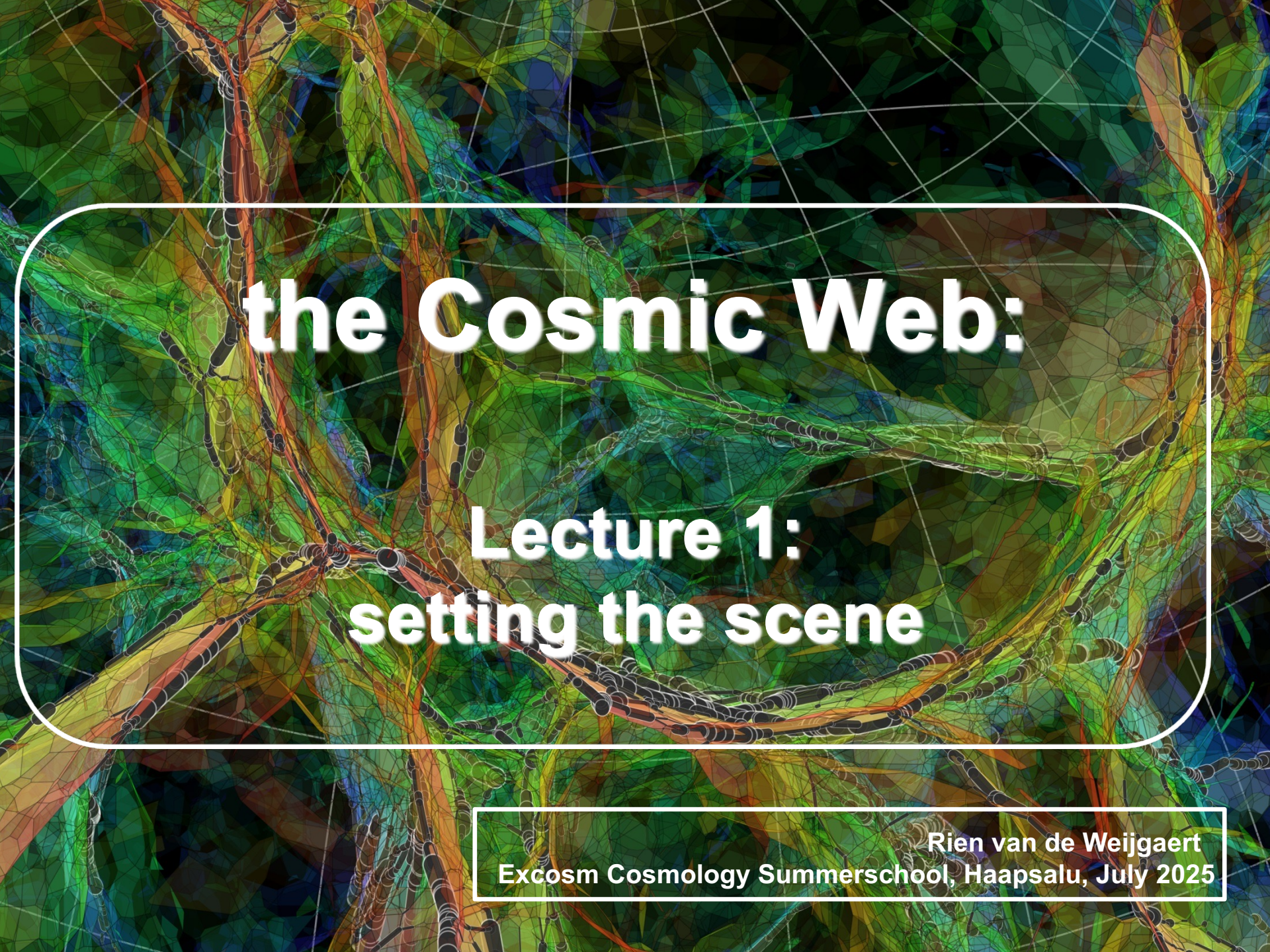


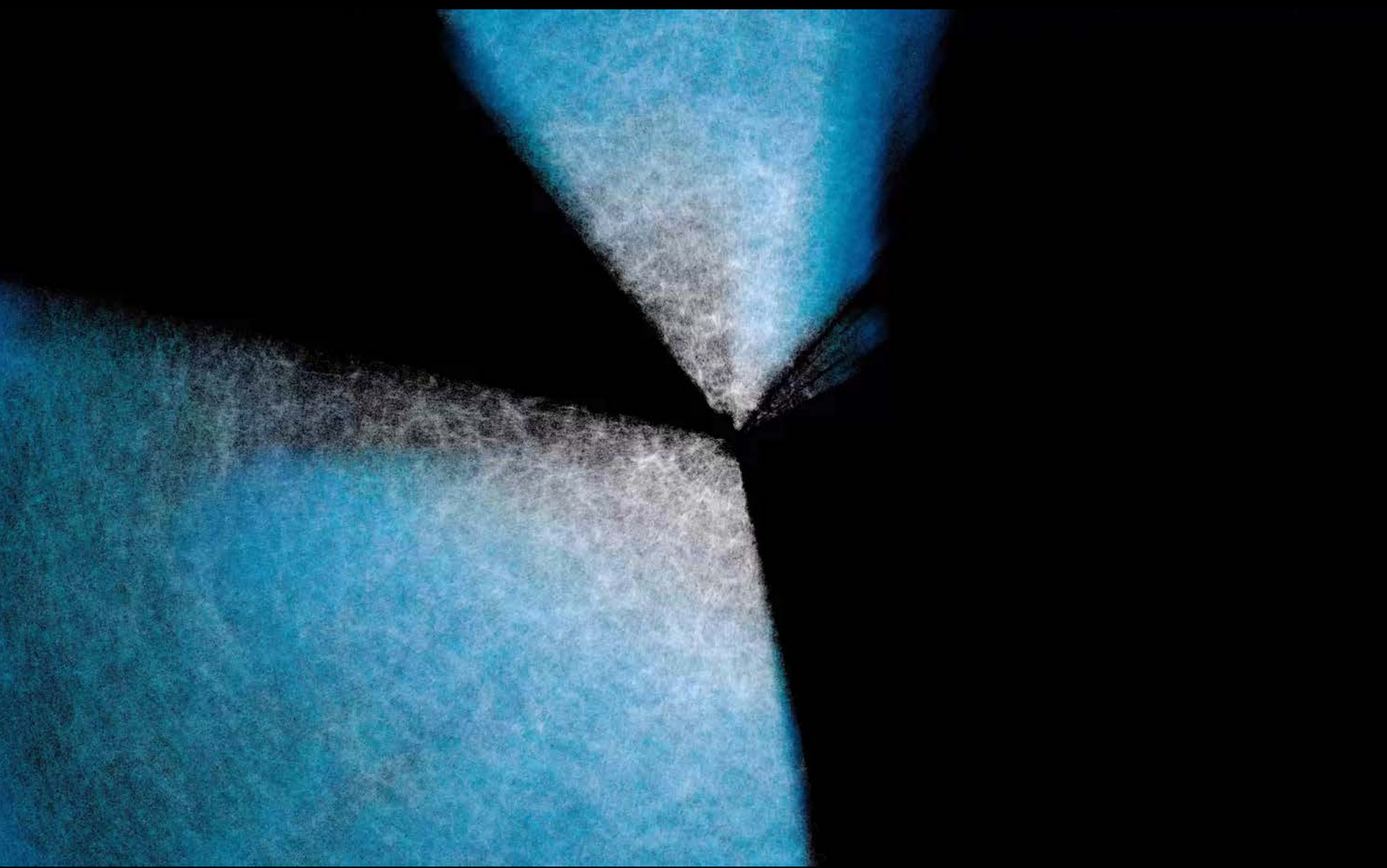
A complex visualization of the cosmic web, showing a dense network of filaments and nodes. The filaments are colored in vibrant shades of green, yellow, and orange, while the nodes are marked with black dots. The background is a dark, textured field of green and blue, suggesting the distribution of dark matter and gas in the universe.

the Cosmic Web:

Lecture 1: setting the scene

Rien van de Weijgaert
Excsm Cosmology Summerschool, Haapsalu, July 2025

Cosmic Web: today's (DESI) view



Cosmic Web Characteristics

- **anisotropic structure:**

- filaments dominant structural feature - elongated
- sheets/walls - flattened

- **multiscale nature**

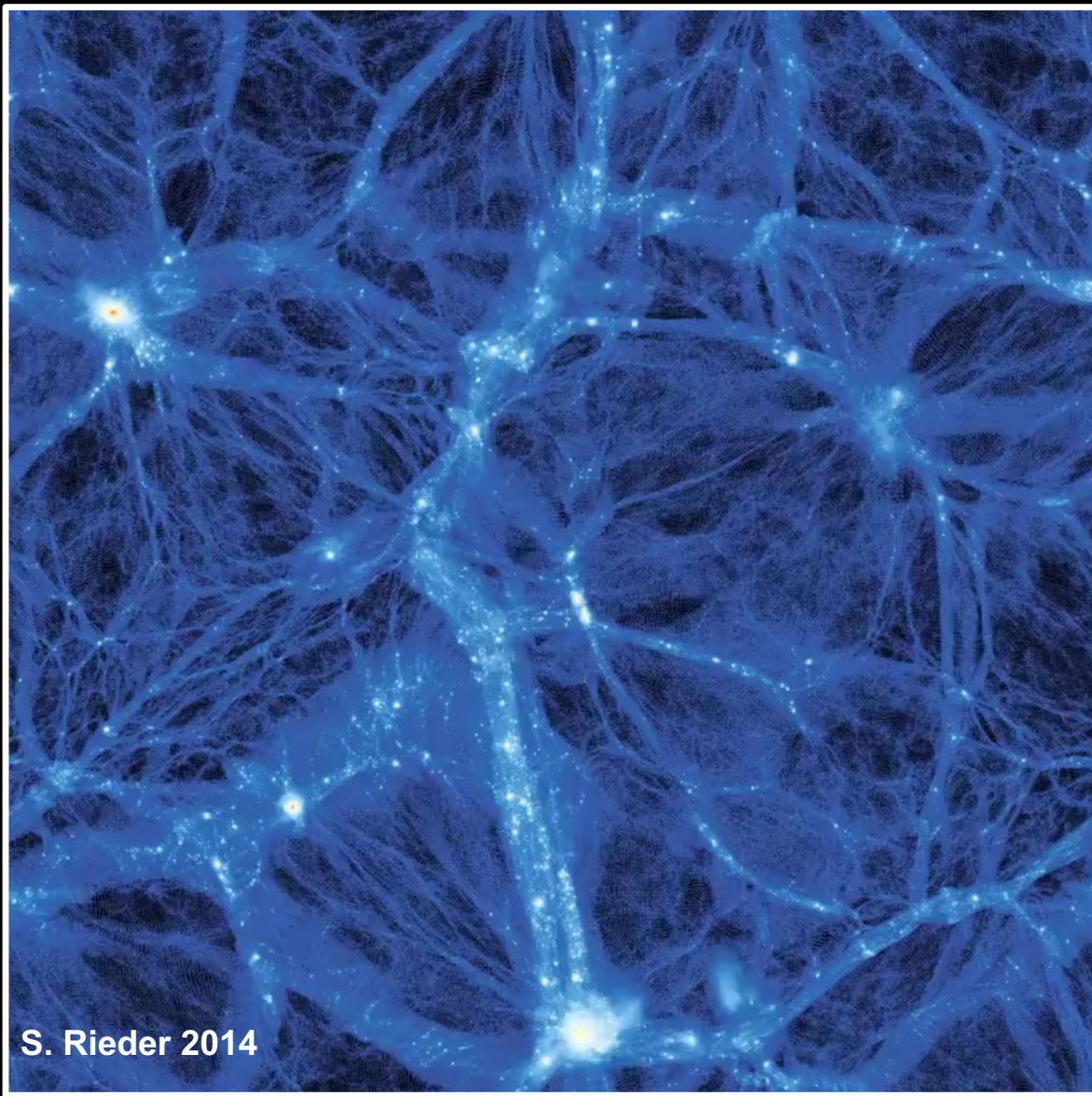
- structure on wide range of scales
- structures have wide range of densities

- **overdense-underdense asymmetry**

- voids: underdense, large & roundish
- filaments & walls: overdense, flattened/elongated
- clusters: dense, massive & compact nodes

- **complex spatial connectivity**

- all structural features connected in a complex, multiscale weblike network



S. Rieder 2014

on scales of $\sim 5\text{-}100\text{s Mpc}$

complex weblike pattern

in which
matter, gas & galaxies
aggregate in

- compact clusters,
 - elongated filaments
 - flattened sheets
- around
- cosmic voids

Cosmic Web

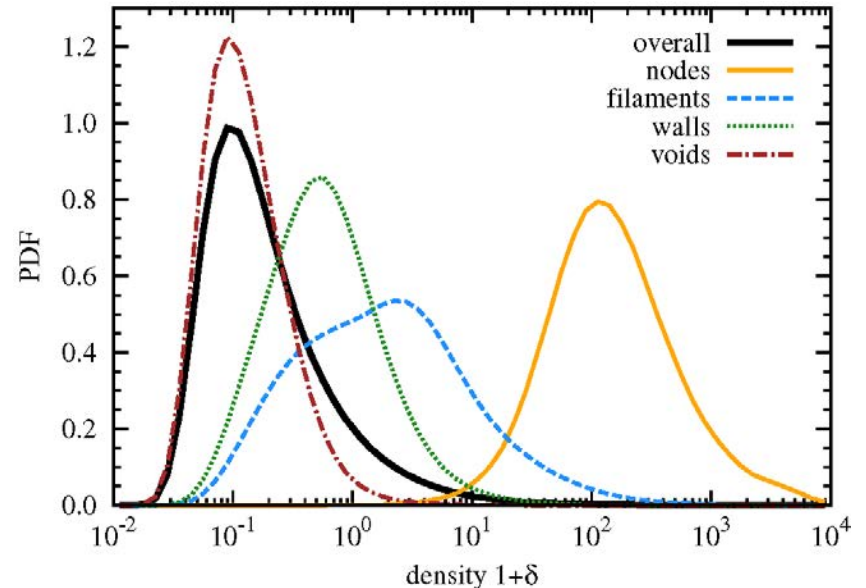
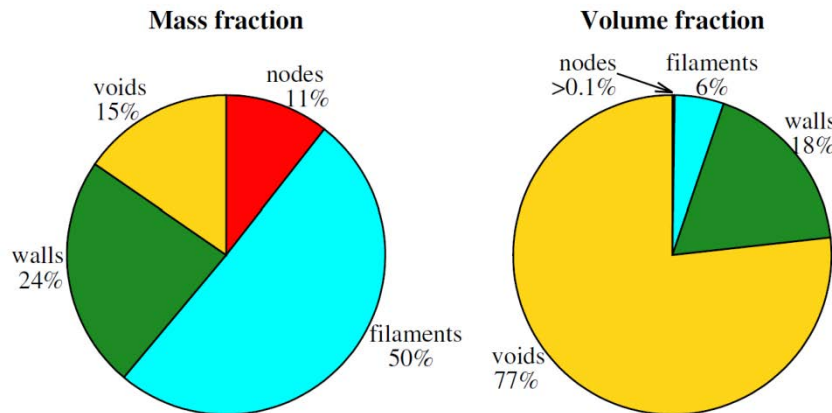
Cosmic Web:

Density-Morphology Connection

Mass & Volume content
Web morphologies



Density distribution
Individual morphologies



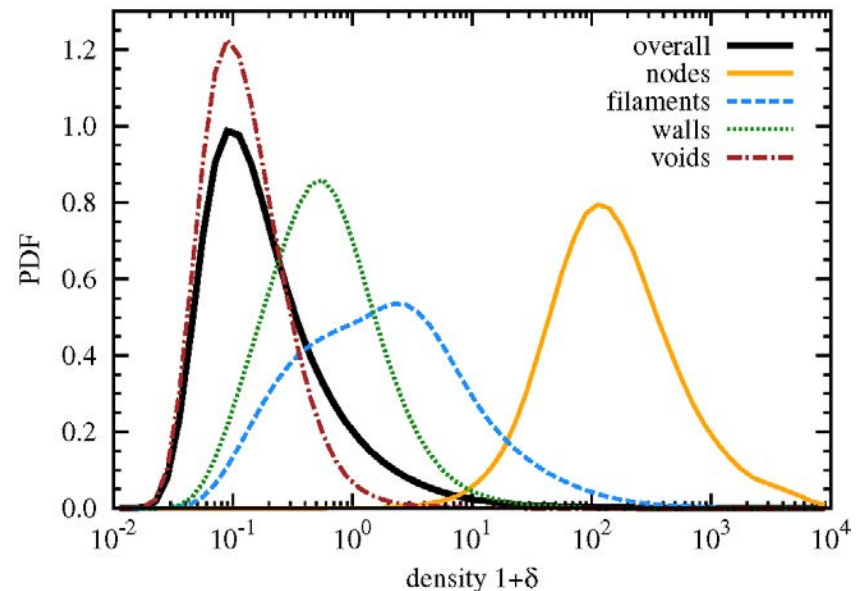
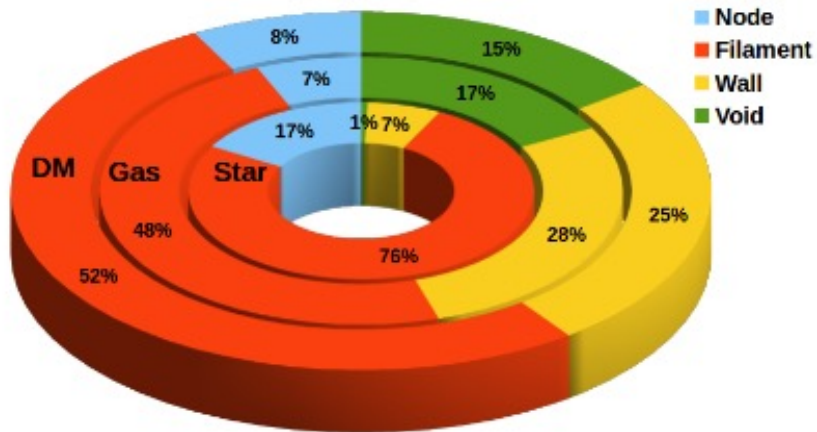
Cosmic Web:

Density-Morphology Connection

Mass & Volume fraction
Web structures



Mass density distribution
Web structures



Cosmic Web

Setting the Scene

A million galaxies

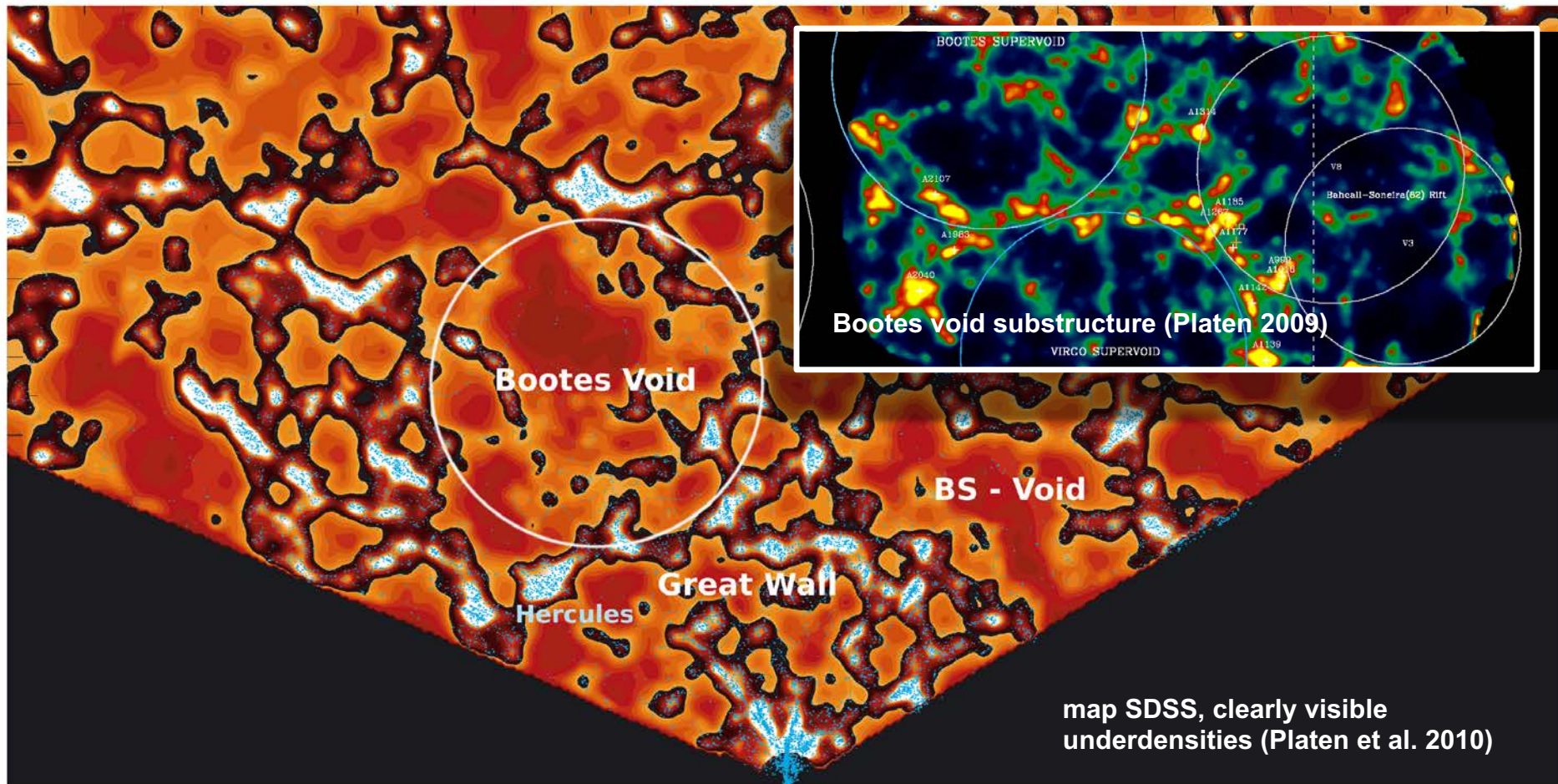
Shane-Wirtanen map:

On the basis of the Shane-Wirtanen counts,

P.J.E. Peebles produced a map of the sky distribution of 1 million galaxies on the sky:

- Clearly visible are clusters
- hint of filamentary LSS features, embedding clusters

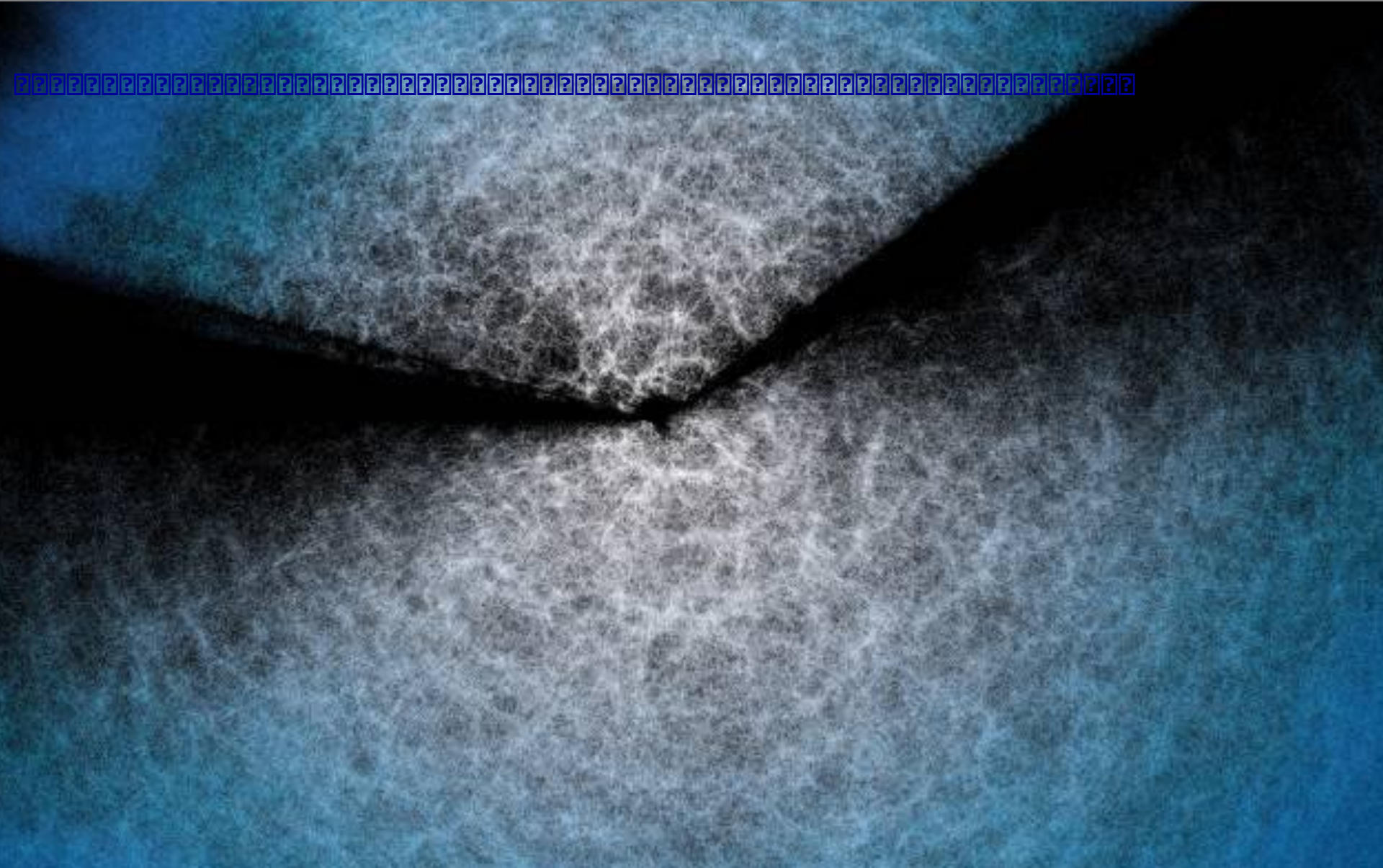
SDSS Galaxy Survey



map SDSS, clearly visible
underdensities (Platen et al. 2010)

with the advent of large galaxy redshift surveys
– LCRS, 2dFGRS, SDSS, 2MRS –
voids have been recognized as one of the quintessential components of the Cosmic Web

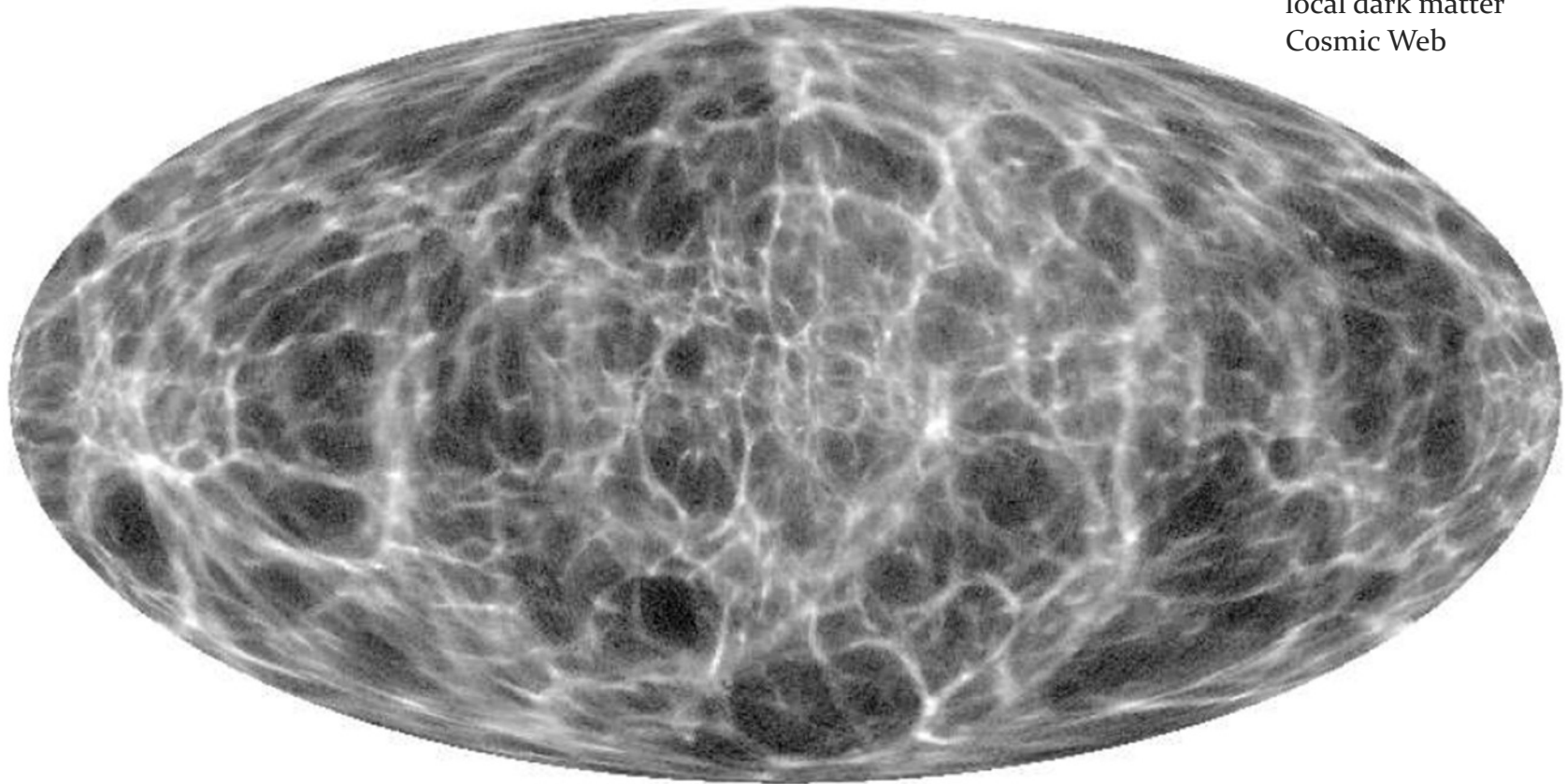
DESI Galaxy Survey



local DM Cosmic Web: 2MRS

most detailed reconstruction
of the

local dark matter
Cosmic Web



1.0 6.0

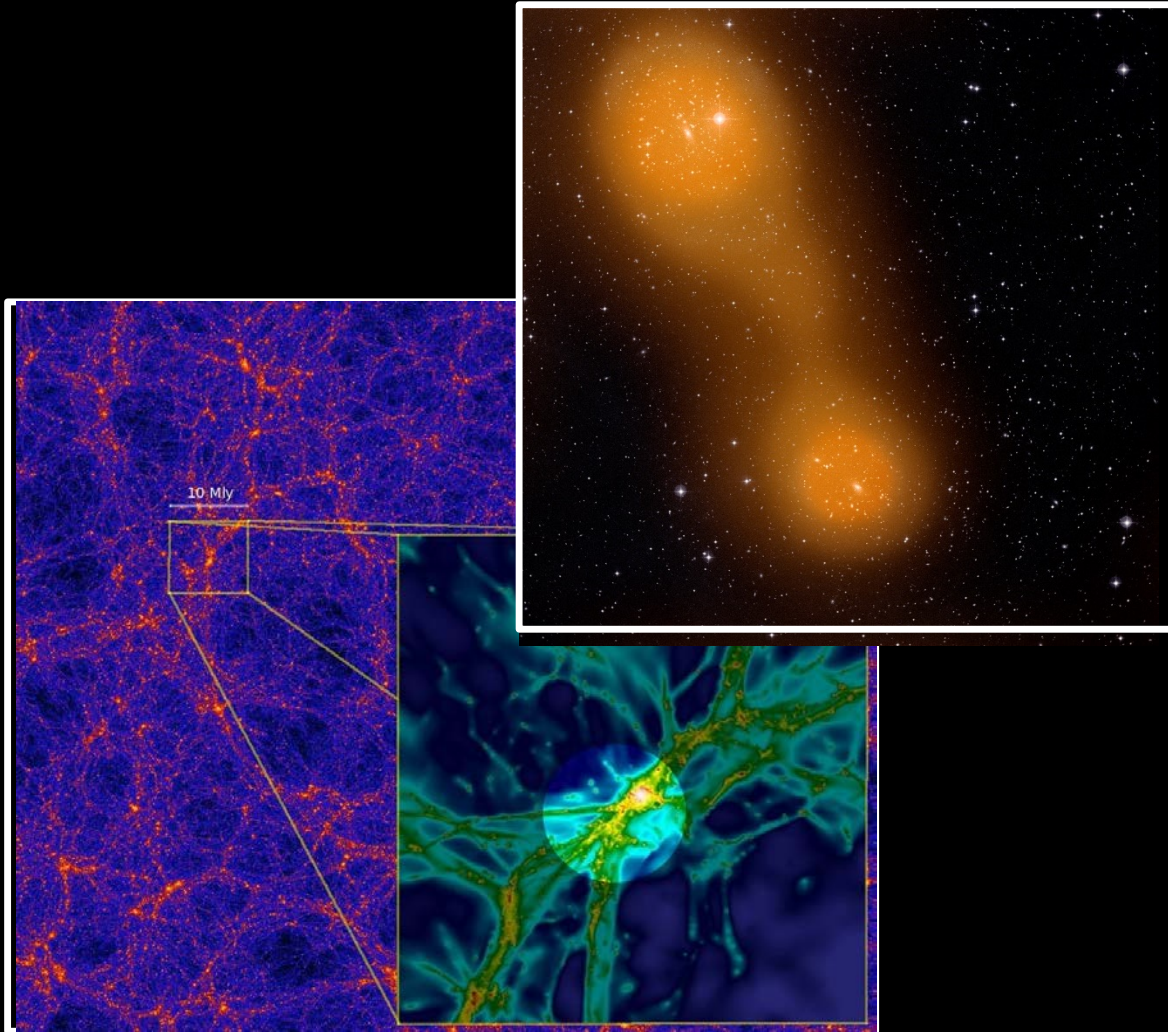
Courtesy: Francisco Kitaura

Cosmic Web: Dark Matter vs Gas

A visualization of the Cosmic Web from the Illustris simulation. The image shows a complex network of dark matter filaments and gas. The dark matter is represented by a blue, fibrous structure on the left side, while the gas is shown as a dense, orange and yellow structure on the right. A central region features a bright, multi-colored core with green and purple hues, indicating high energy or temperature. The overall background is black, emphasizing the intricate web of matter.

Illustris Simulation

the Gaseous Cosmic Web



Gaseous Cosmic Web:

Detection via:

- 1) Ly α absorption (Ly α forest)
 - neutral hydrogen (cloud)
 - mostly at high redshift
 - absorption against quasar los.
 - possible use as tomographic tool
- 2) WHIM
 - warm-hot intergalactic medium
 - soft Xray emission of hot gas (10^5 K)
very hard to see
 - absorption lines Xray band (eg. OVI)
- 3) Sunyaev-Zeldovich scattering filaments
 - inverse Compton scattering
CMB photons against hot electrons
in ICM/IGM
 - has been seen in Planck (80 filam.):
 - bridges between clusters

Cosmic Web in Cosmic History

Cosmic Web in Cosmic History



→ COSMIC HISTORY

10⁻³² seconds

1 second

100 seconds

380 000 years

300–500 million years

Billions of years

13.8 billion years

Beginning
of the
Universe



Inflation

Accelerated expansion
of the Universe

Formation of light and matter

Light and matter are coupled

Dark matter evolves
independently: it starts
clumping and forming
a web of structures

Light and matter separate

- Protons and electrons
form atoms
- Light starts travelling
freely: it will become the
Cosmic Microwave

Dark ages

Atoms start feeling
the gravity of the
cosmic web of dark
matter

First stars

The first stars and
galaxies form in the
densest knots of the
cosmic web

Galaxy evolution

The present Universe

Cosmic Web at Cosmic Dawn



→ COSMIC HISTORY



10^{-32} seconds

1 second

100 seconds

380 000 years

300–500 million years

Billions of years

13.8 billion years

Beginning
of the
Universe

Inflation

Accelerated expansion
of the Universe

Formation of light and matter

100 seconds

380 000 years

300–500 million years



Light and matter are coupled

Dark matter evolves
independently; it starts
clumping and forming
a web of structures

Light and matter separate

- Protons and electrons
form atoms
- Light starts travelling
freely; it will become the
Cosmic Microwave
Background (CMB)

Dark ages

Atoms start feeling
the gravity of the
cosmic web of dark
matter

First stars

The first stars and
galaxies form in the
densest knots of the
cosmic web

The present Universe

Cosmic Web in Later Universe



→ COSMIC HISTORY



10⁻³² seconds

1 second

100 seconds

380 000 years

300–500 million years

Billions of years

13.8 billion years

Beginning
of the
Universe

Inflation

Accelerated expansion
of the Universe

Formation of light and matter

300–500 million years

Billions of years

13.8 billion years

The present Universe

Dark ages

Atoms start feeling
the gravity of the
cosmic web of dark
matter

First stars

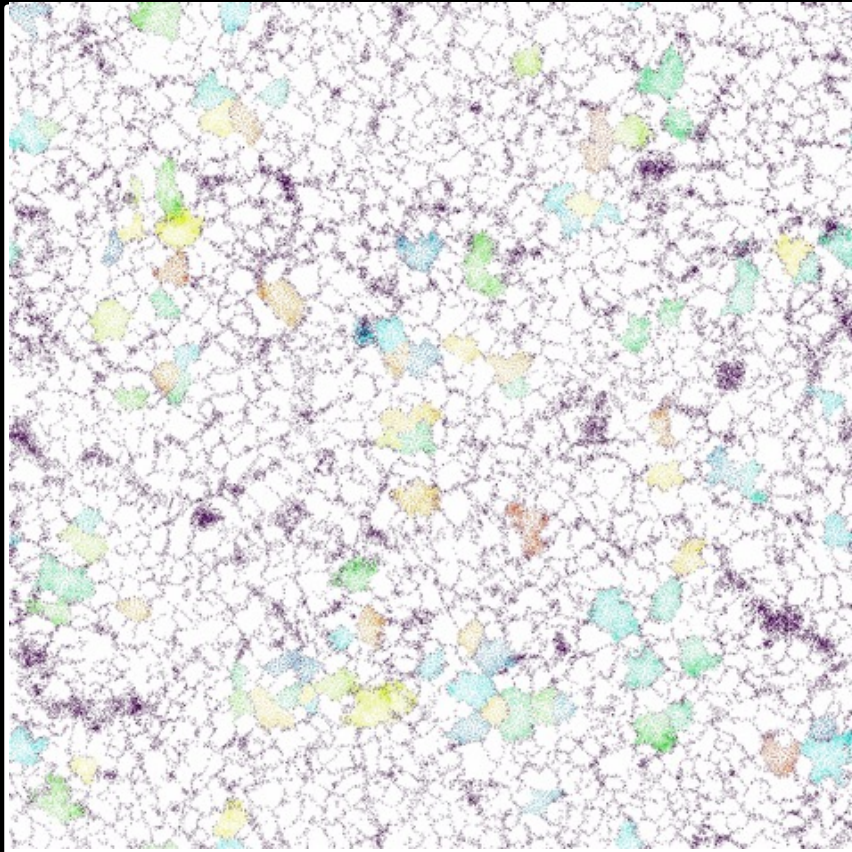
The first stars and
galaxies form in the
densest knots of the
cosmic web

Galaxy evolution

The present Universe

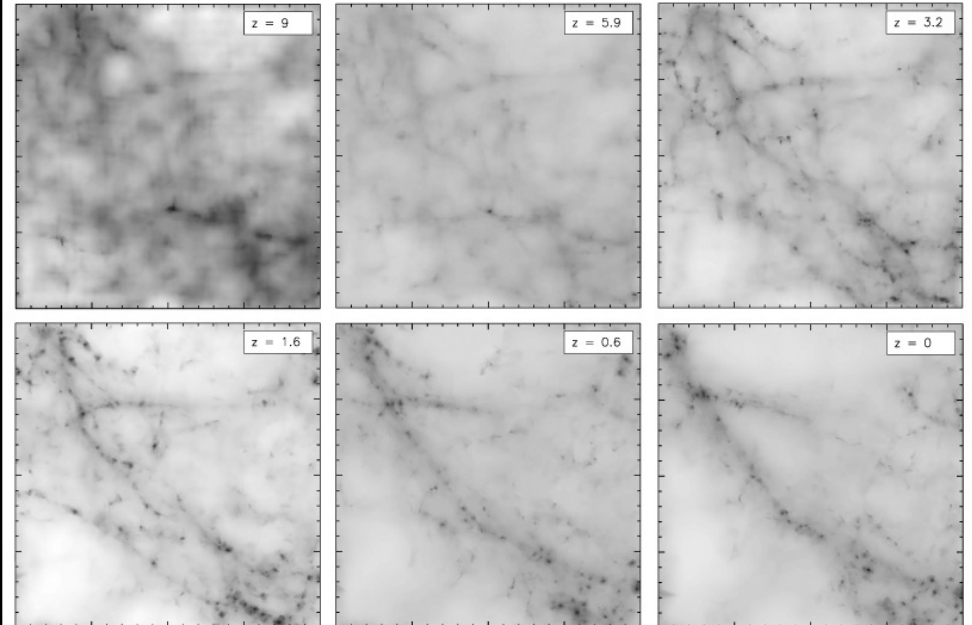
Hierarchical Buildup Cosmic Web

Adhesion formalism allows the geometric modelling of the hierarchical buildup of the cosmic web



Platen & vdW 2004
Sheth & vdW 2004
Aragon-Calvo & Szalay 2012

Hierarchy of Voids

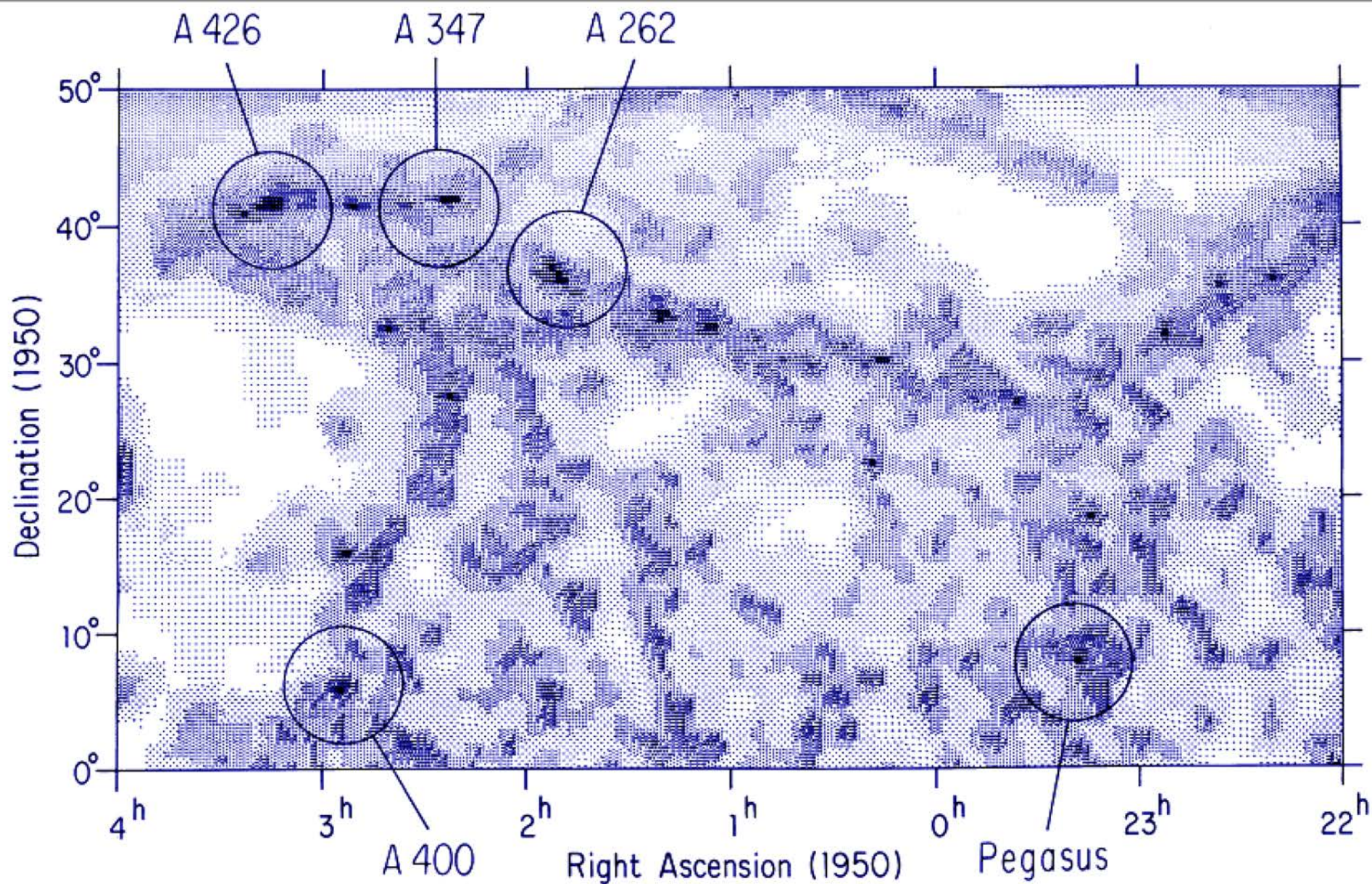


Hierarchy of Filaments
Aragon-Calvo 2007

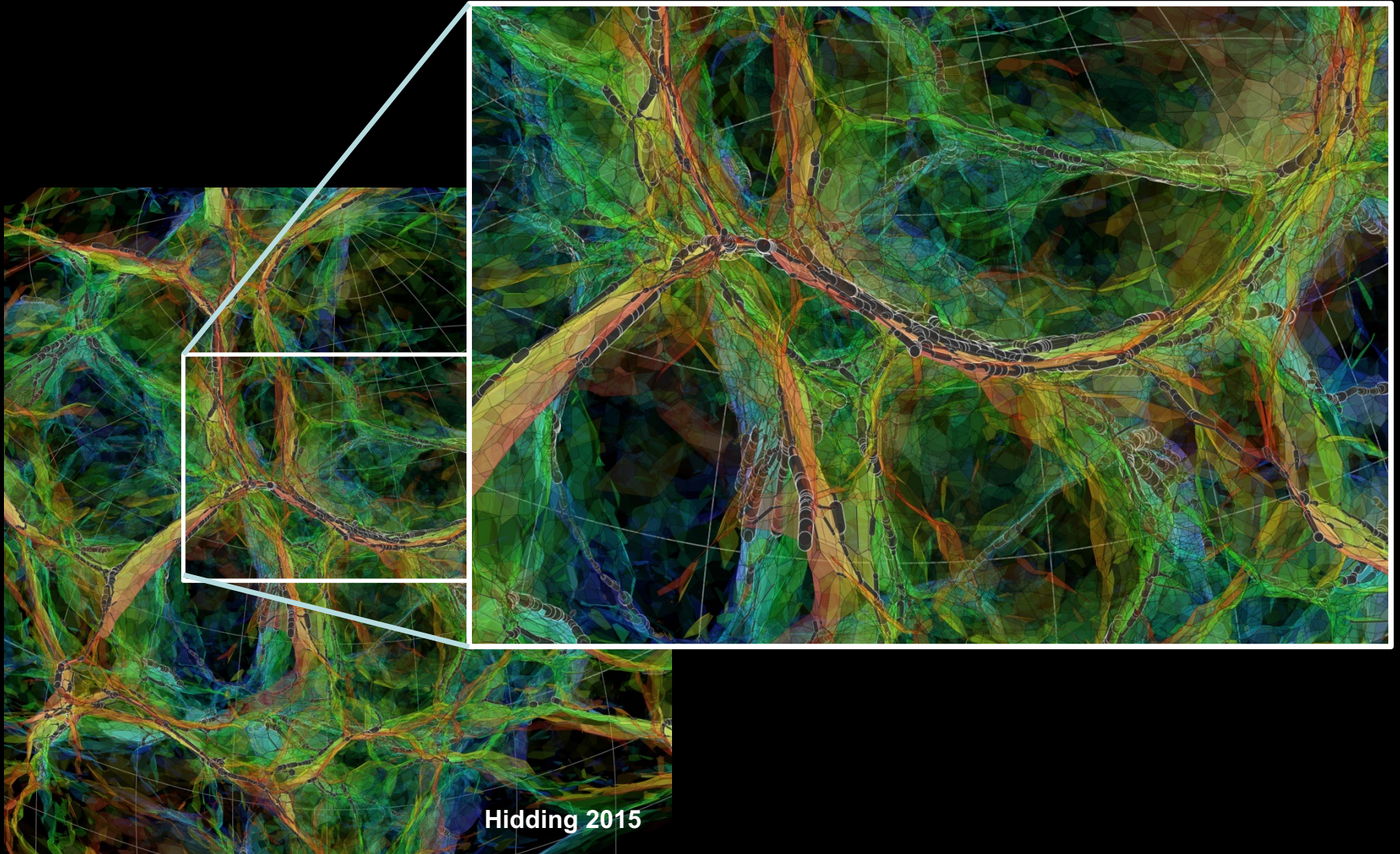
Cosmic Web

Characteristics

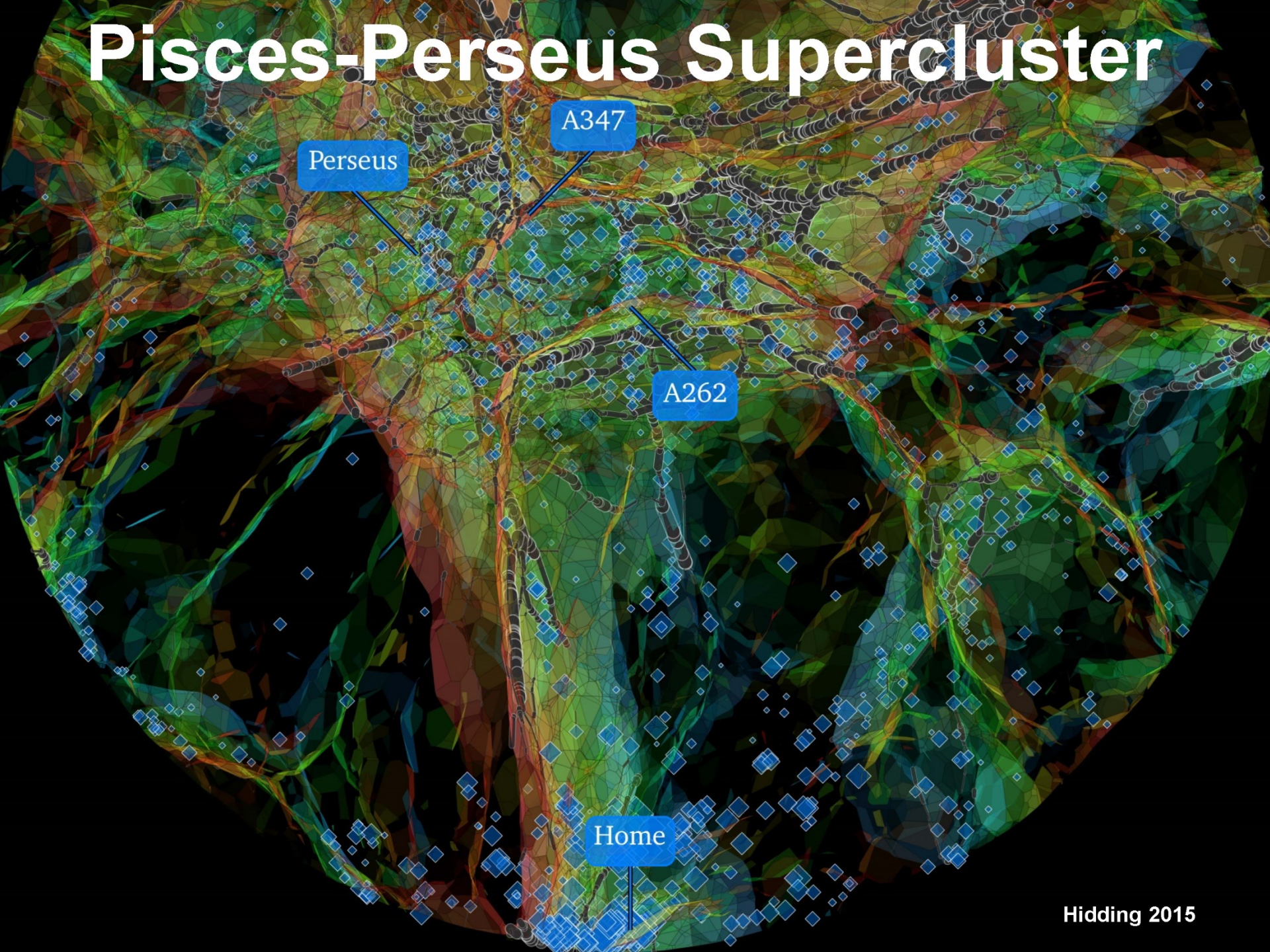
Pisces-Perseus Supercluster



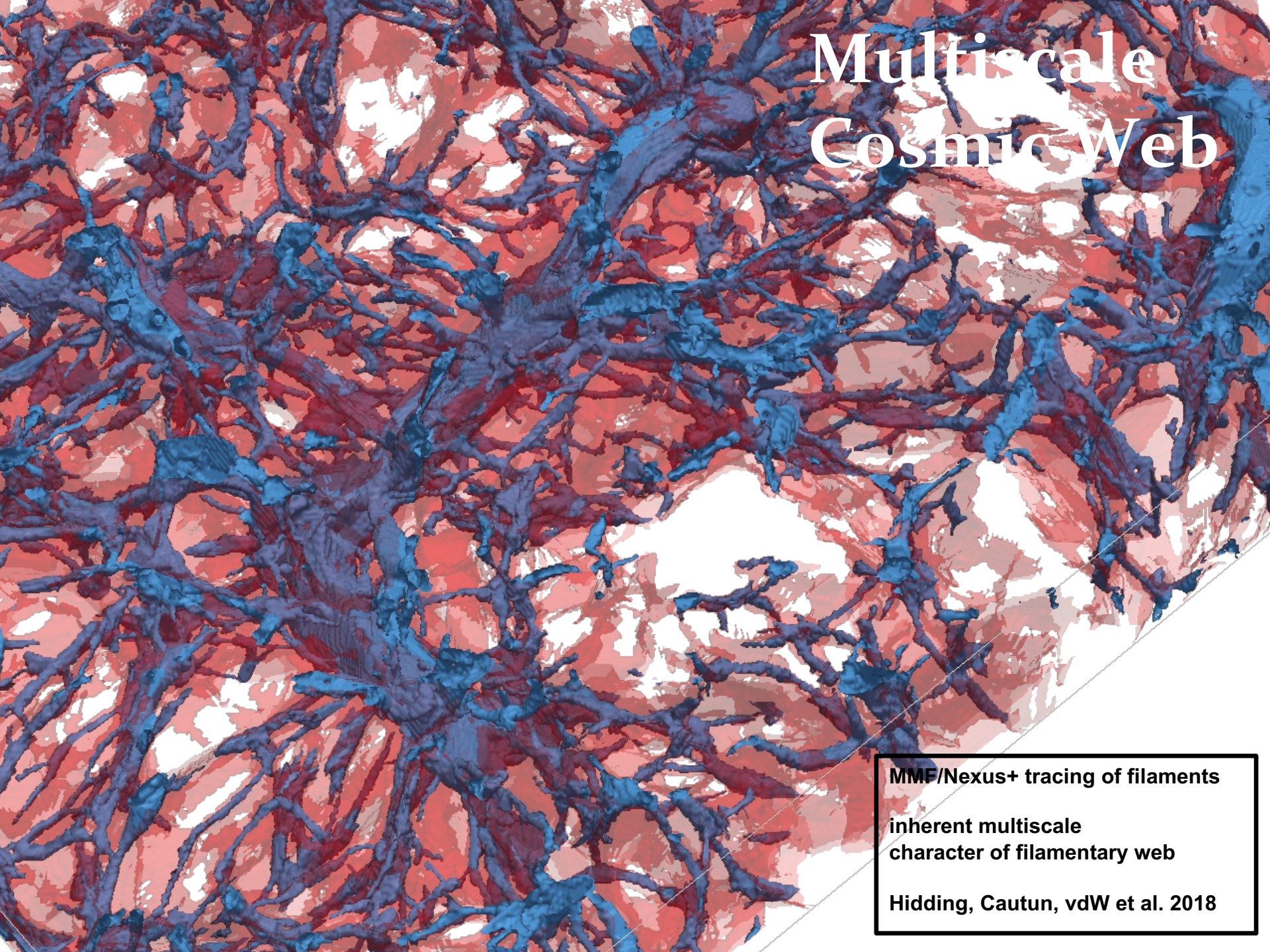
Pisces-Perseus Supercluster



Pisces-Perseus Supercluster



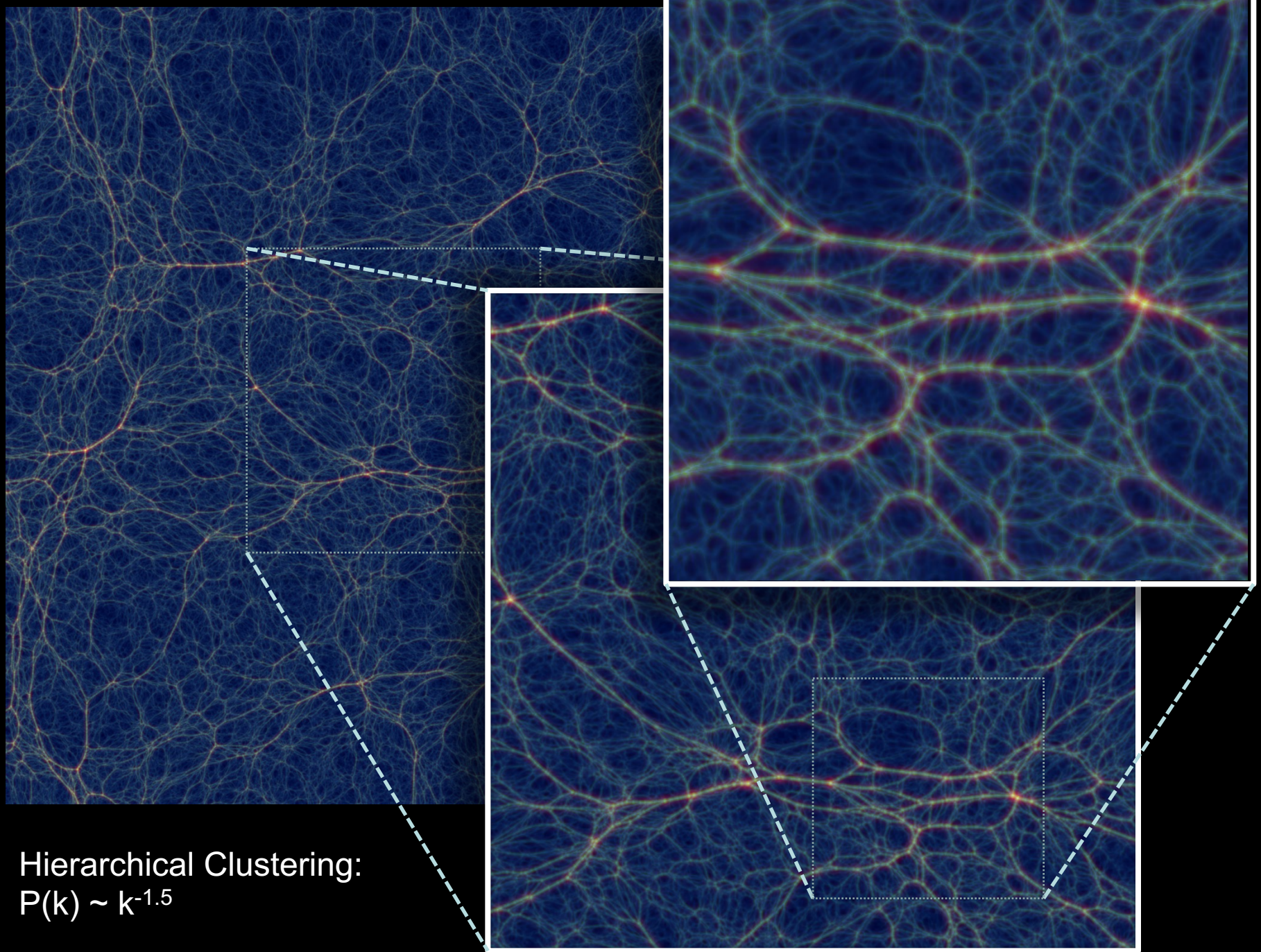
Multiscale Cosmic Web

A 3D visualization of the Cosmic Web, showing a dense network of blue filaments and nodes against a red and white background. The filaments are complex and interconnected, forming a web-like structure. The background is a mix of red and white, with some areas appearing more saturated than others.

MMF/Nexus+ tracing of filaments

inherent multiscale
character of filamentary web

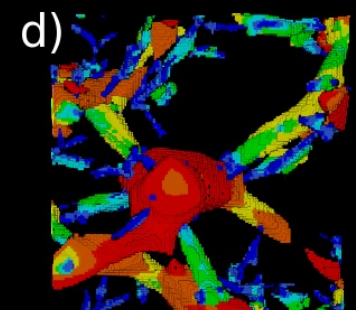
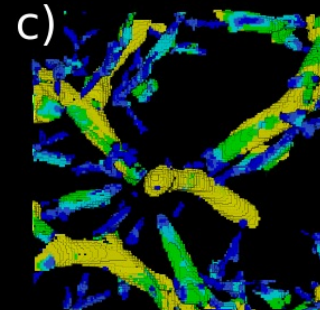
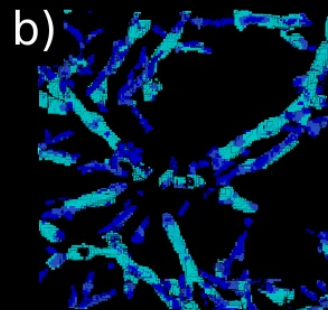
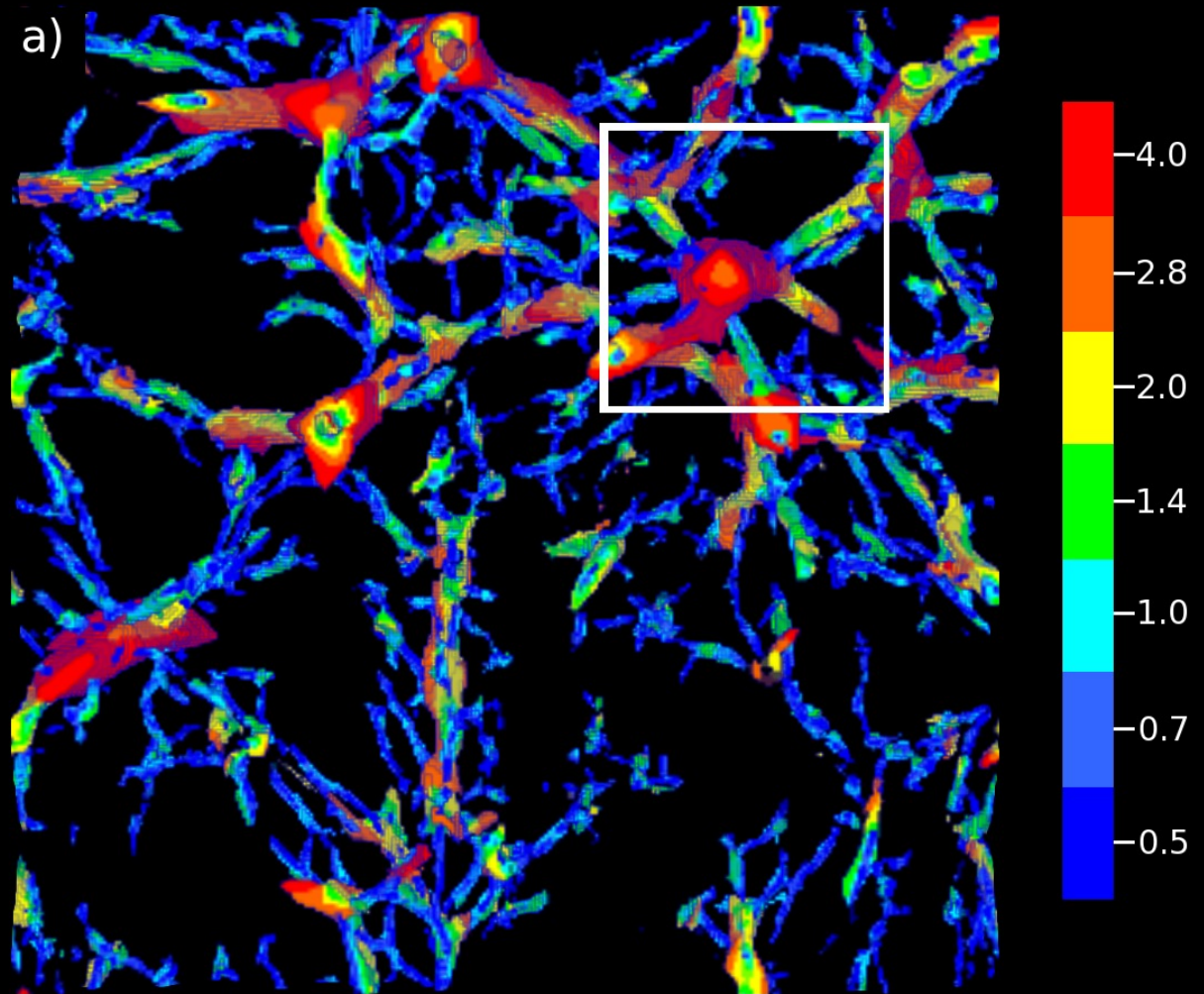
Hidding, Cautun, vdW et al. 2018



Nexus:

Multiscale
Morphology
Identification

Filaments



Colouring :
Local scale filament

Cosmic Voids

- Voids are prominent aspects of the Cosmic Web, instrumental in spatial organization of the Megaparsec Universe.

Sheth & van de Weygaert 2004

Hidding, van de Weygaert, Kitaura & Hess 2015

- Voids contain significant amount of information on global cosmological parameters:
 - void outflow: dark matter
 - void shapes: dark energy
 - supervoids: existence

Bos, van de Weygaert, Dolag & Pettorino 2012

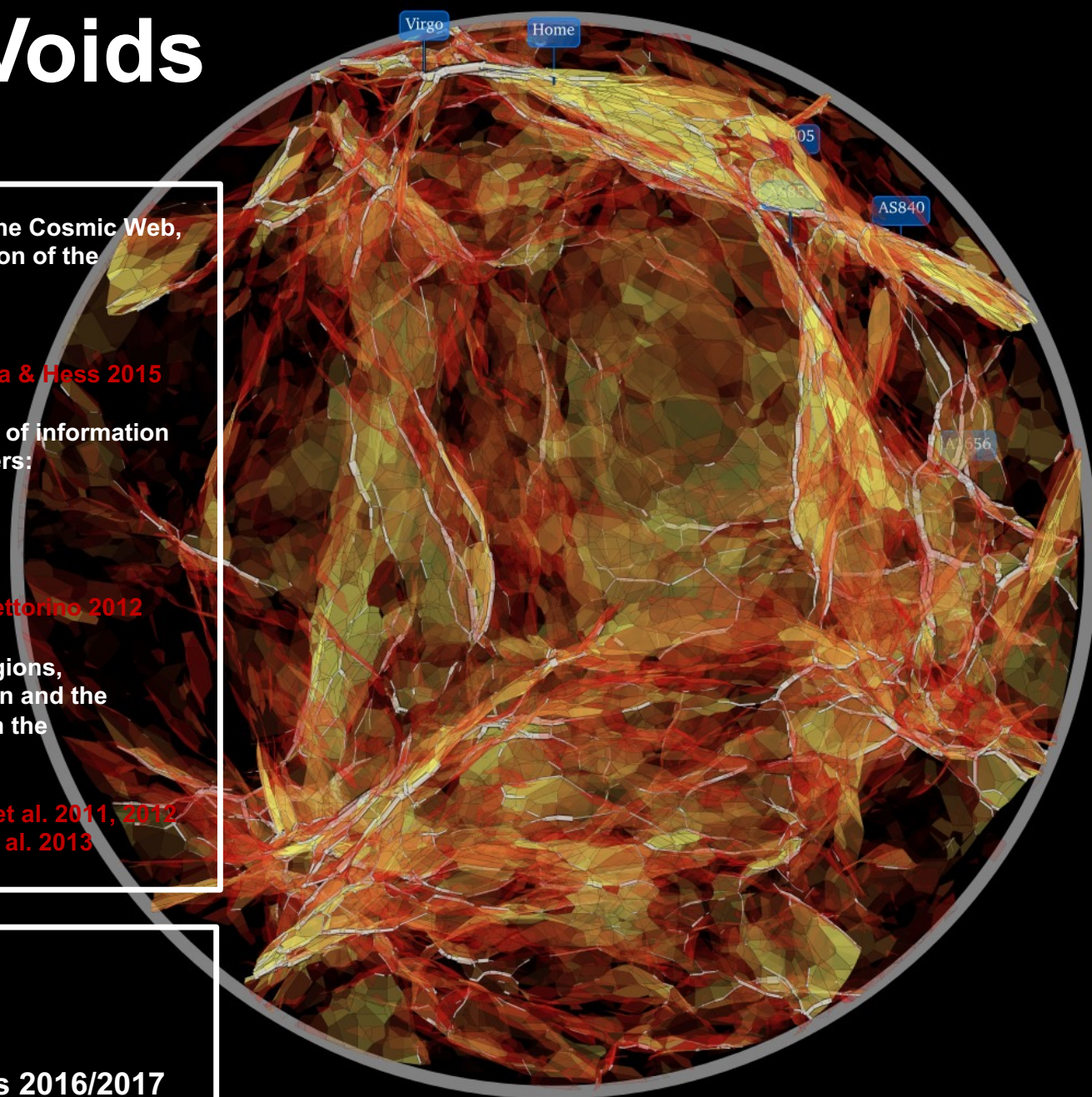
- Voids are pristine low-density regions, ideal for studying galaxy formation and the effects of cosmic environment on the formation of galaxies.

Void Galaxy Survey: Kreckel et al. 2011, 2012
Beygu et al. 2013

Local Void

Reconstruction:

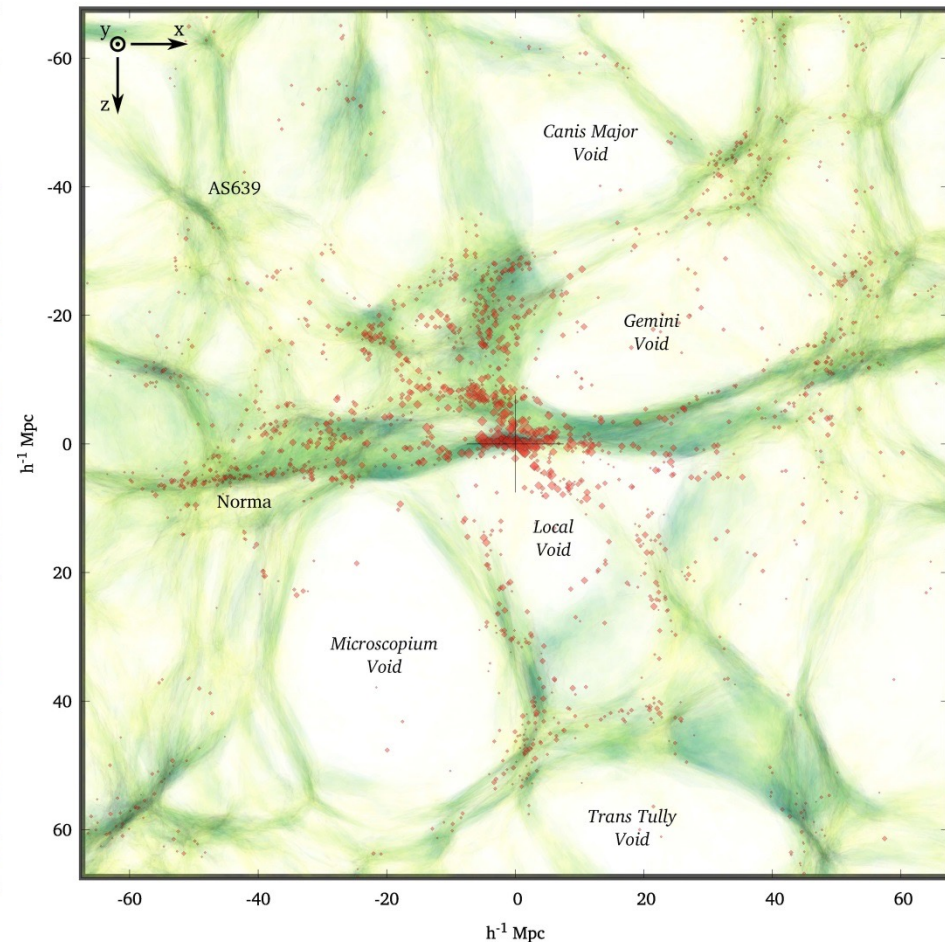
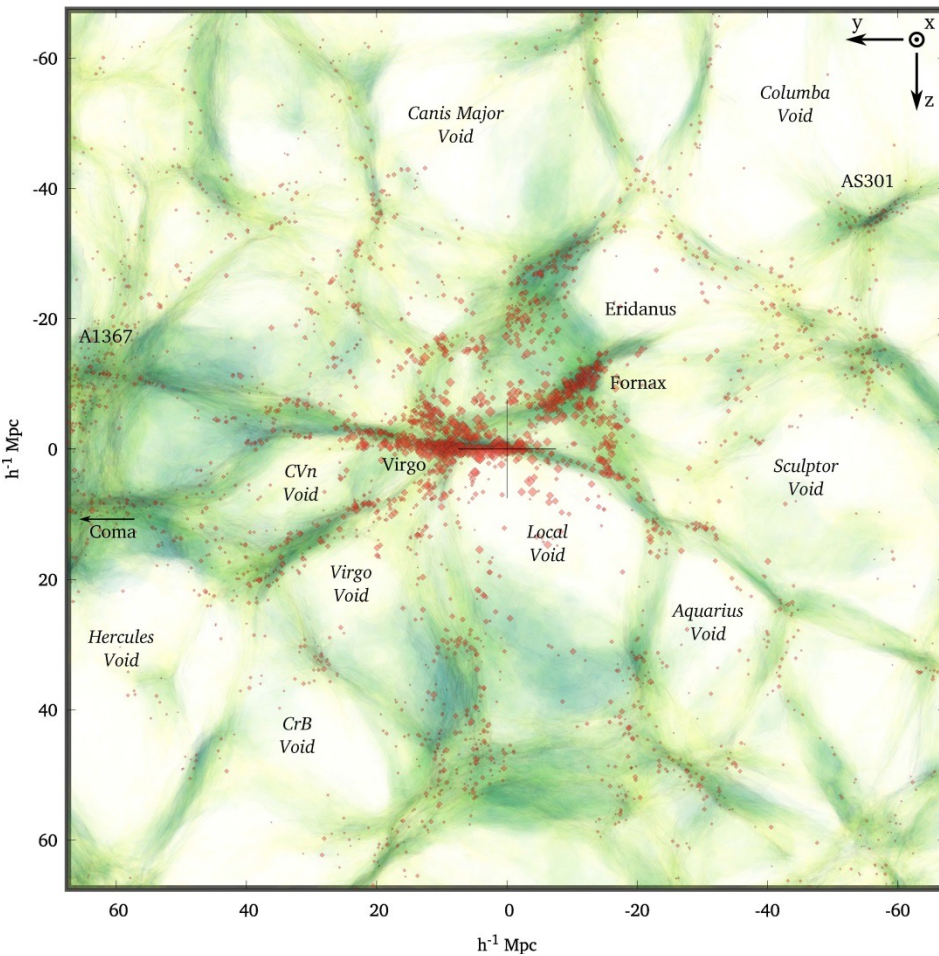
Hidding, vdW, Kitaura & Hess 2016/2017



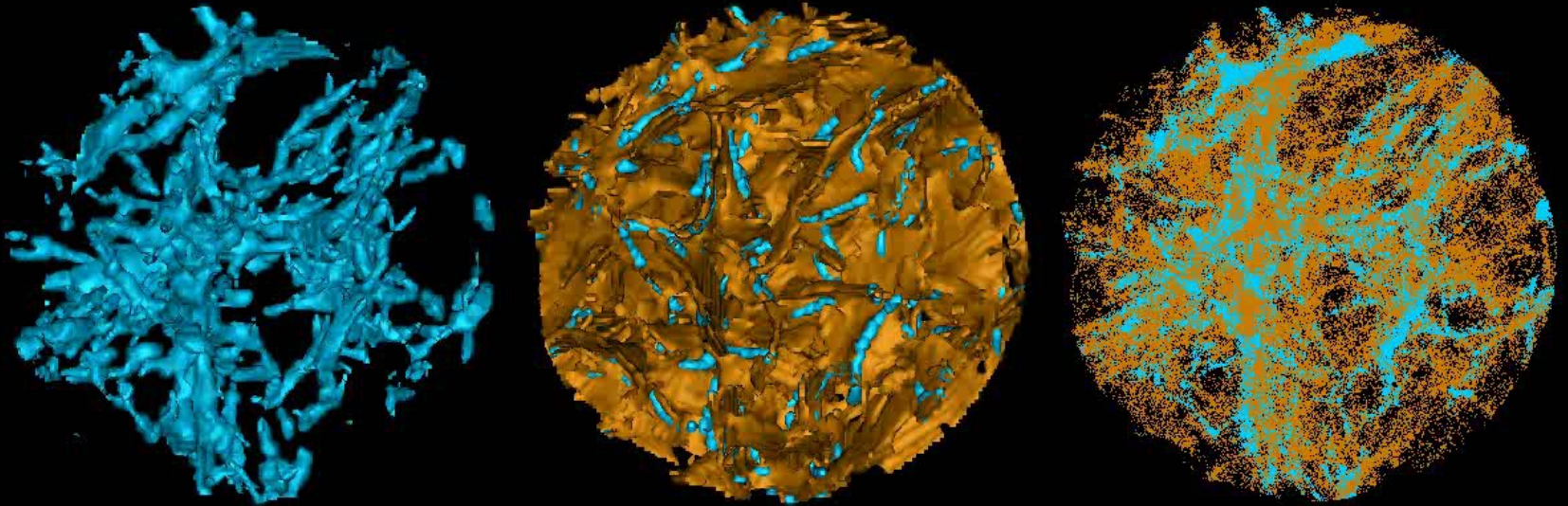
Void Population Local Universe

mean KIGEN-adhesion reconstruction (2MRS)

Hidding, Kitaura, vdW & Hess 2016/2017



Cosmic Web: Connectivity



MMF/Nexus
Cautun et al. 2013, 2014

Stochastic Spatial Pattern

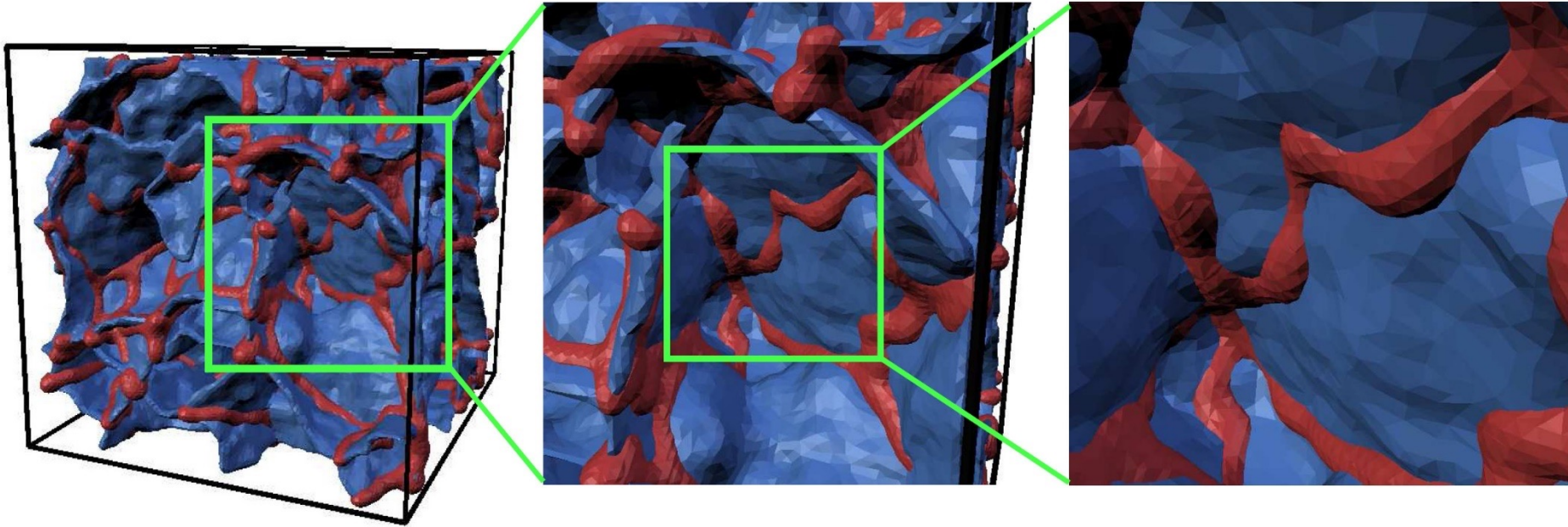
- Clusters,
 - Filaments &
 - Walls
- around
- Voids

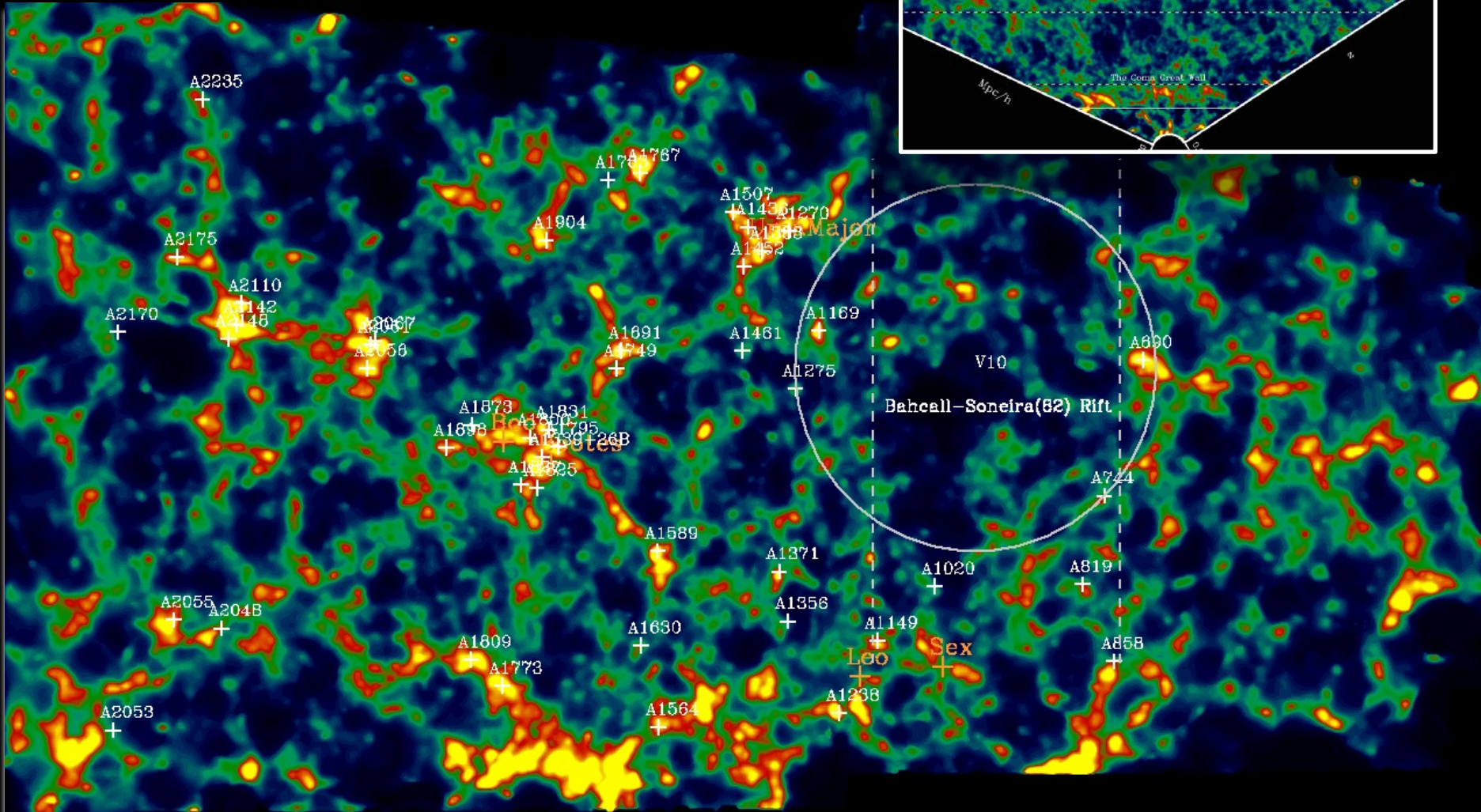
in which matter & galaxies

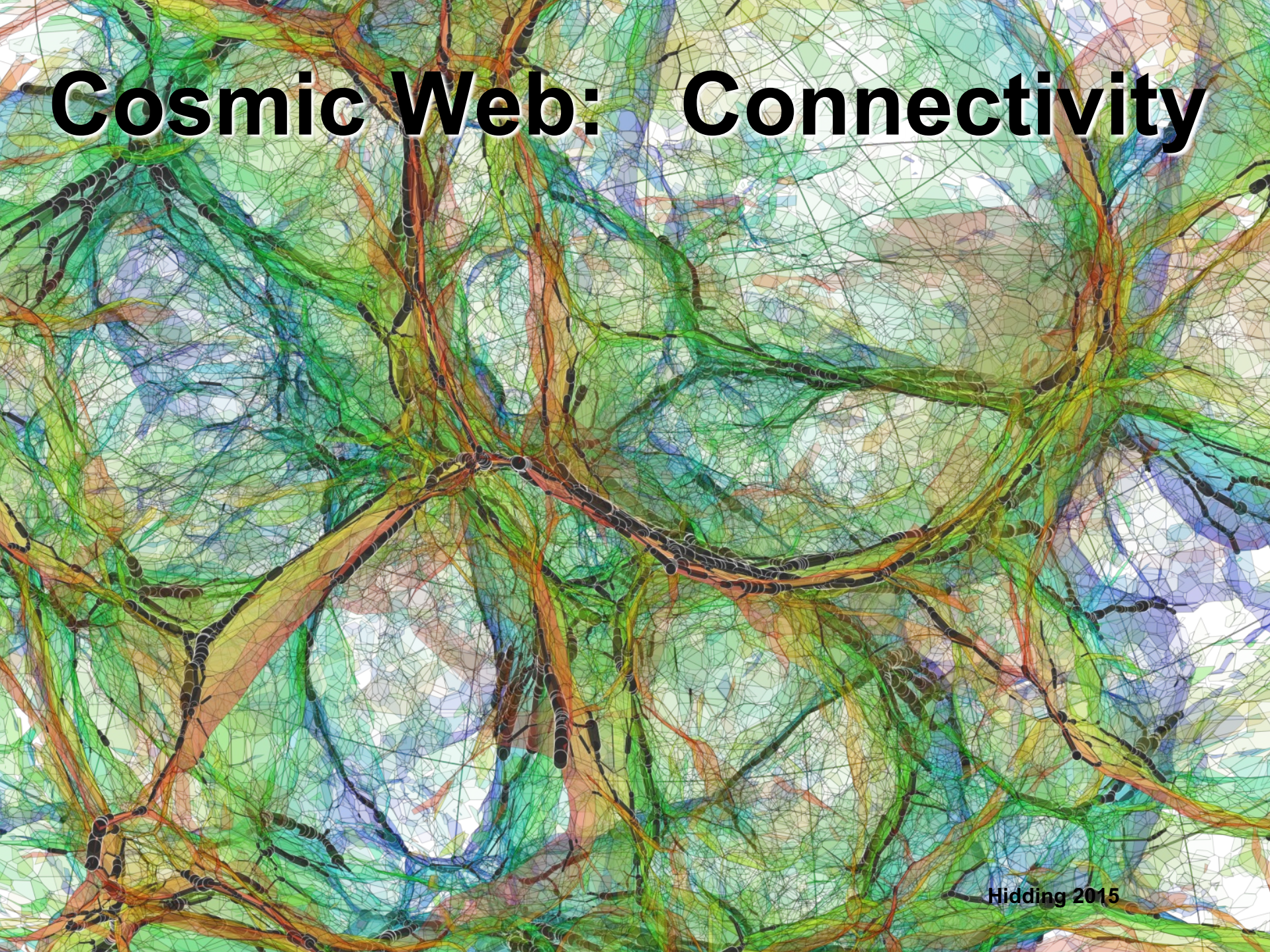
have agglomerated

through gravity

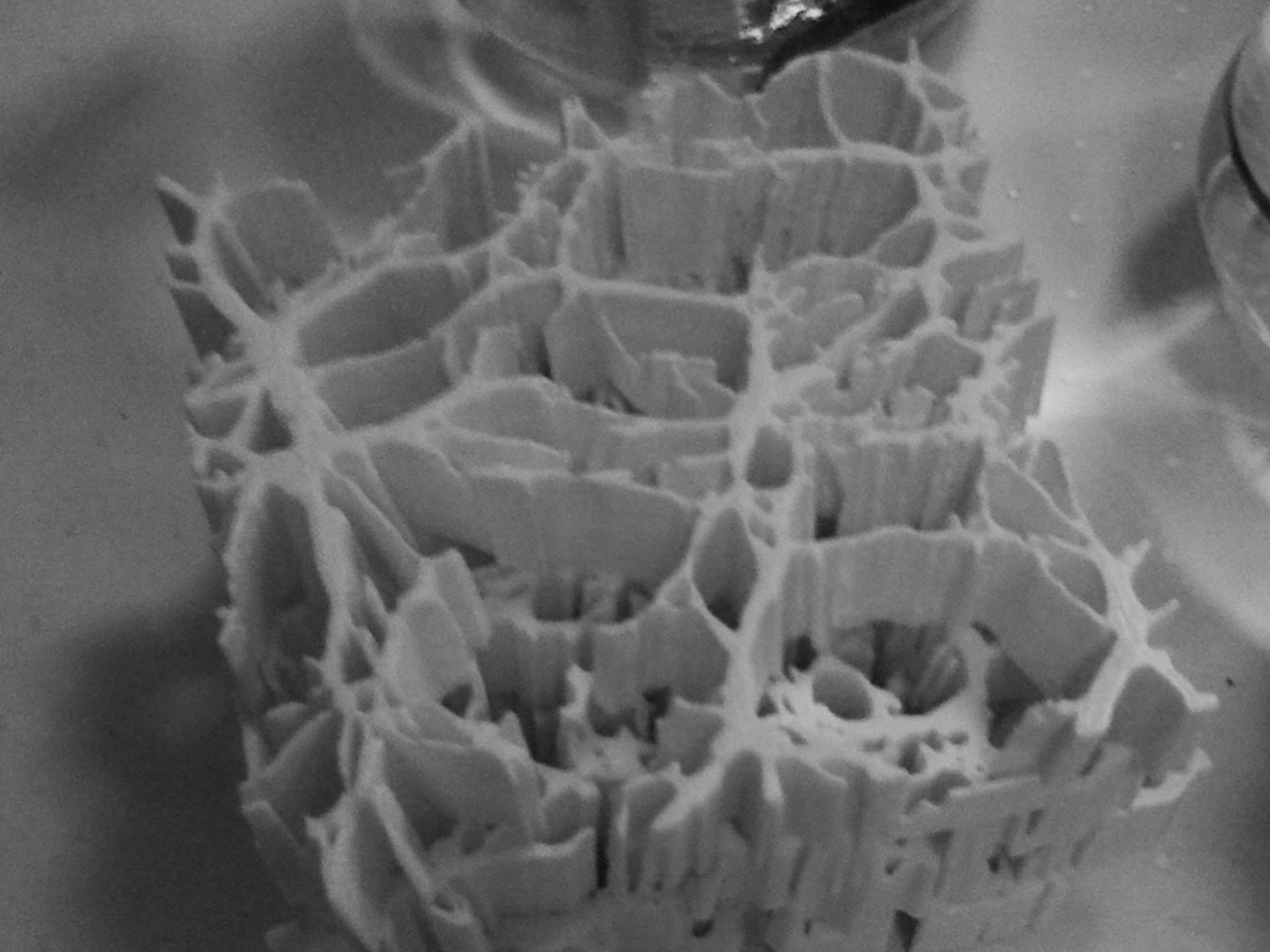
the Network: Walls – Filaments - Nodes







Cosmic Web: Connectivity

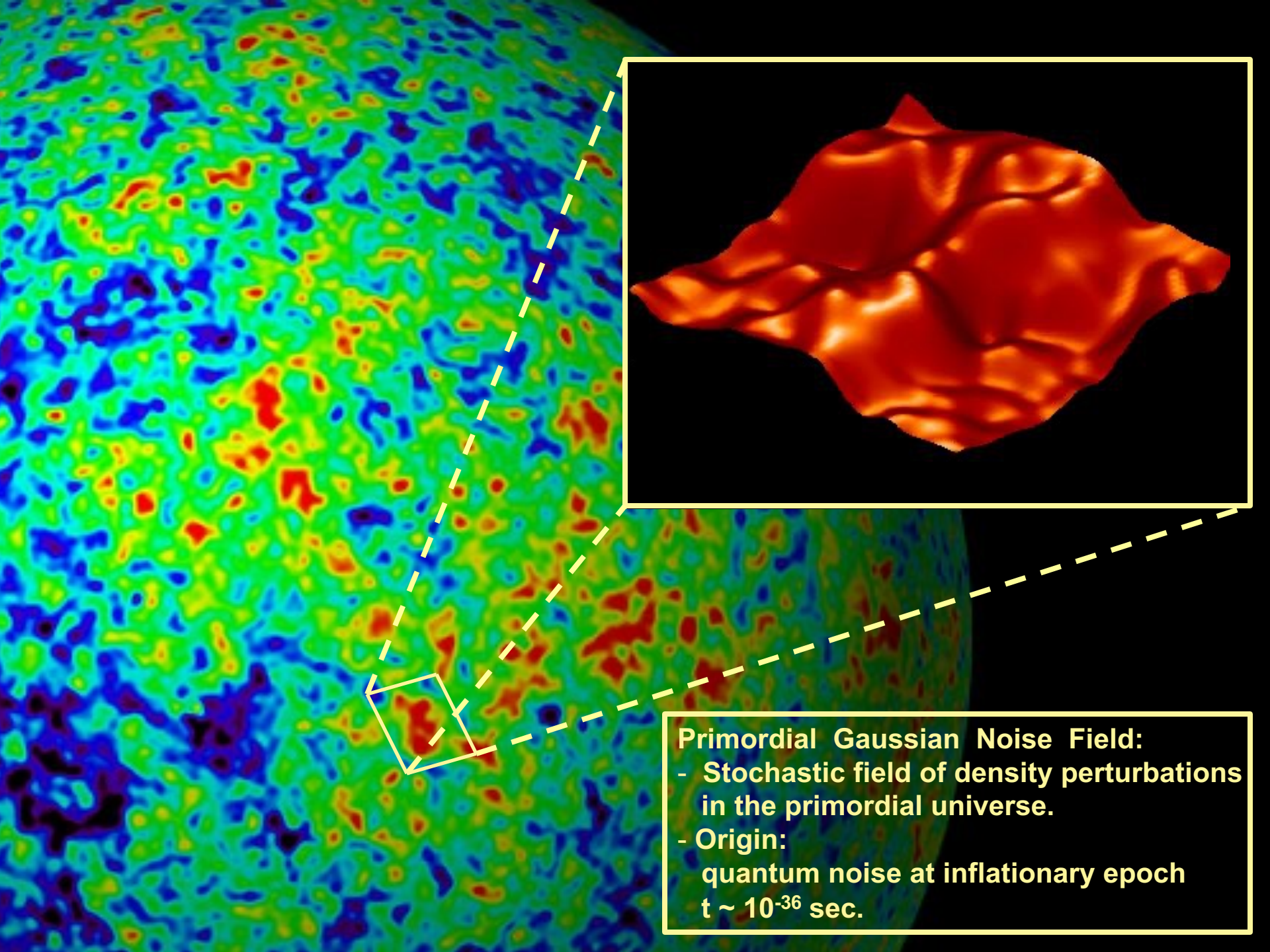


The Cosmic Web

Physical Significance:

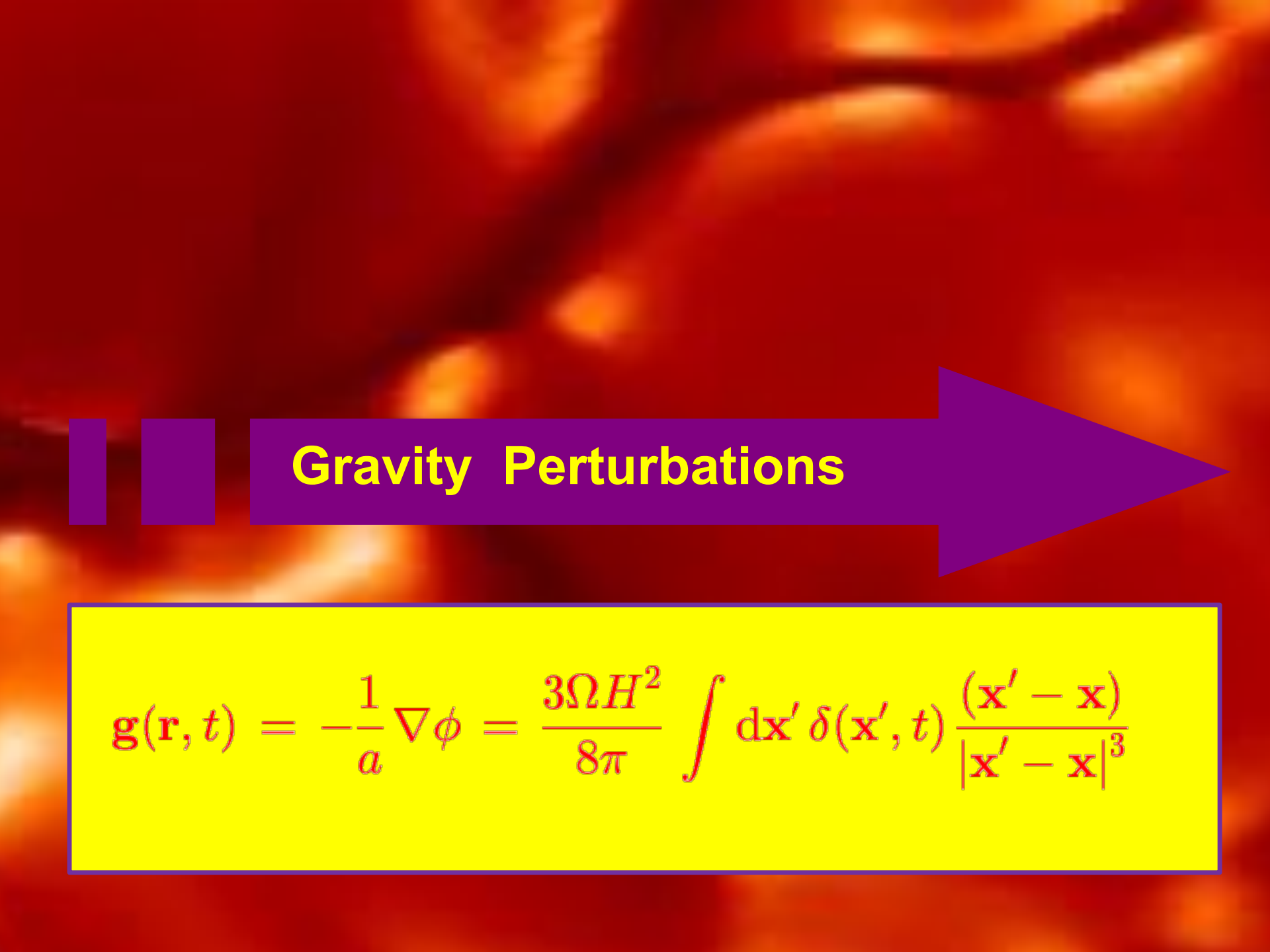
- **Manifestation mildly nonlinear clustering:**
Transition stage between linear phase
and fully collapsed/virialized objects
- **Weblike configurations contain**
cosmological information:
eg. Void shapes & Alignments
- **Cosmic environment within which to understand**
the formation of galaxies.

Cosmic Structure Formation: Gravitational Instability



Primordial Gaussian Noise Field:

- Stochastic field of density perturbations in the primordial universe.
- Origin:
quantum noise at inflationary epoch
 $t \sim 10^{-36}$ sec.



Gravity Perturbations

$$\mathbf{g}(\mathbf{r}, t) = -\frac{1}{a} \nabla \phi = \frac{3\Omega H^2}{8\pi} \int d\mathbf{x}' \delta(\mathbf{x}', t) \frac{(\mathbf{x}' - \mathbf{x})}{|\mathbf{x}' - \mathbf{x}|^3}$$

Cosmic Structure Formation

(Energy) Density Perturbations



Gravity Perturbations



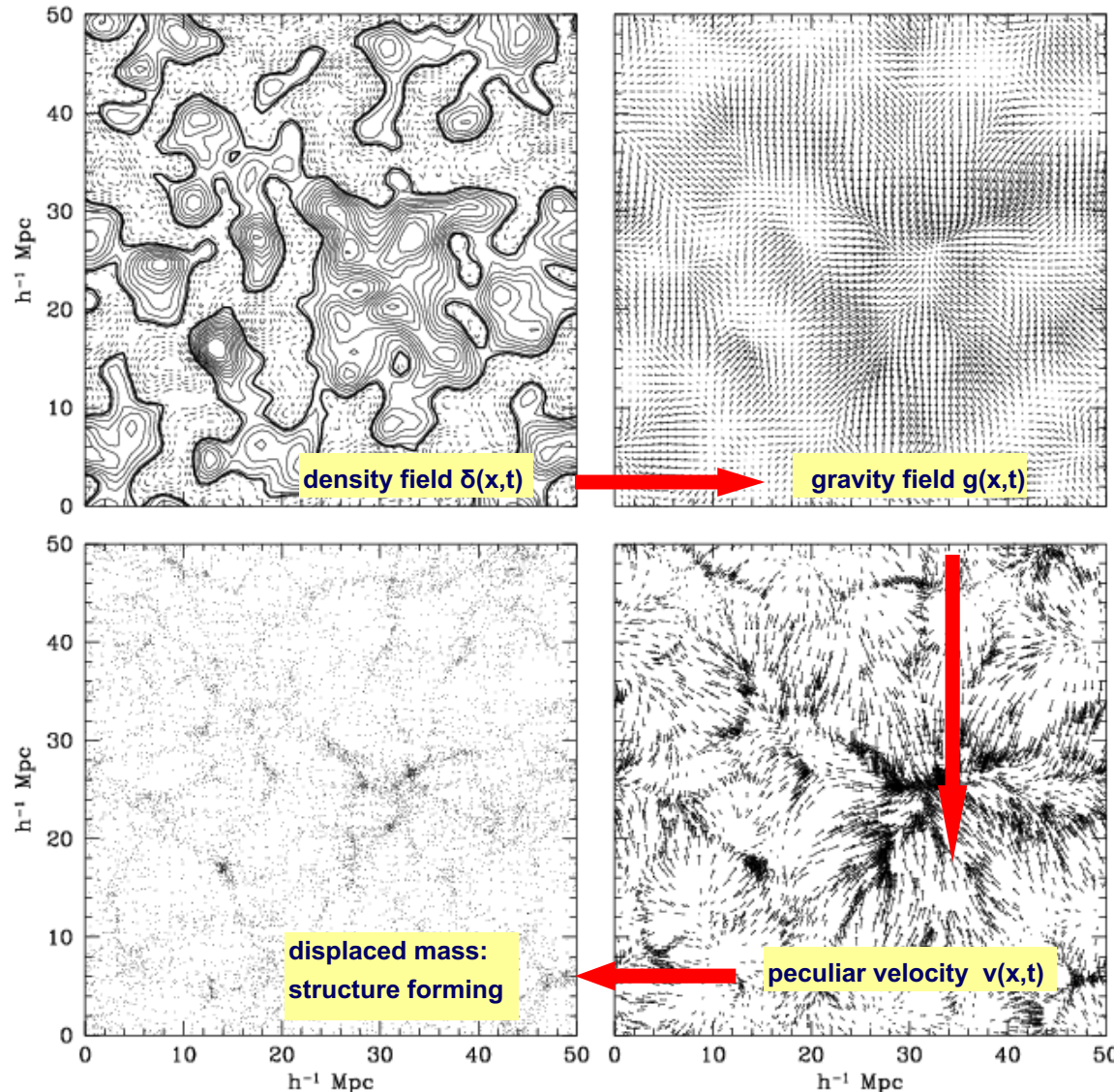
(Cosmic) Flows of (Energy) & Matter:

- ☐ towards high density regions:
 - assemble more and more matter
 - their expansion comes to a halt
 - turn around and collapse
- ☐ evacuating void regions
 - low-density regions expand
 - matter moves out of region
 - turn into prominent empty voids



Emergence of cosmic structures

- ☐ Computer Simulations
 - succesfull confrontation with observational reality



Cosmic Structure Formation

Millennium
Simulation:
LCDM

31.25 Mpc/h

(courtesy:
Virgo/V. Springel).

**Dark Matter,
(~ 5.5x more than
baryonic matter)**



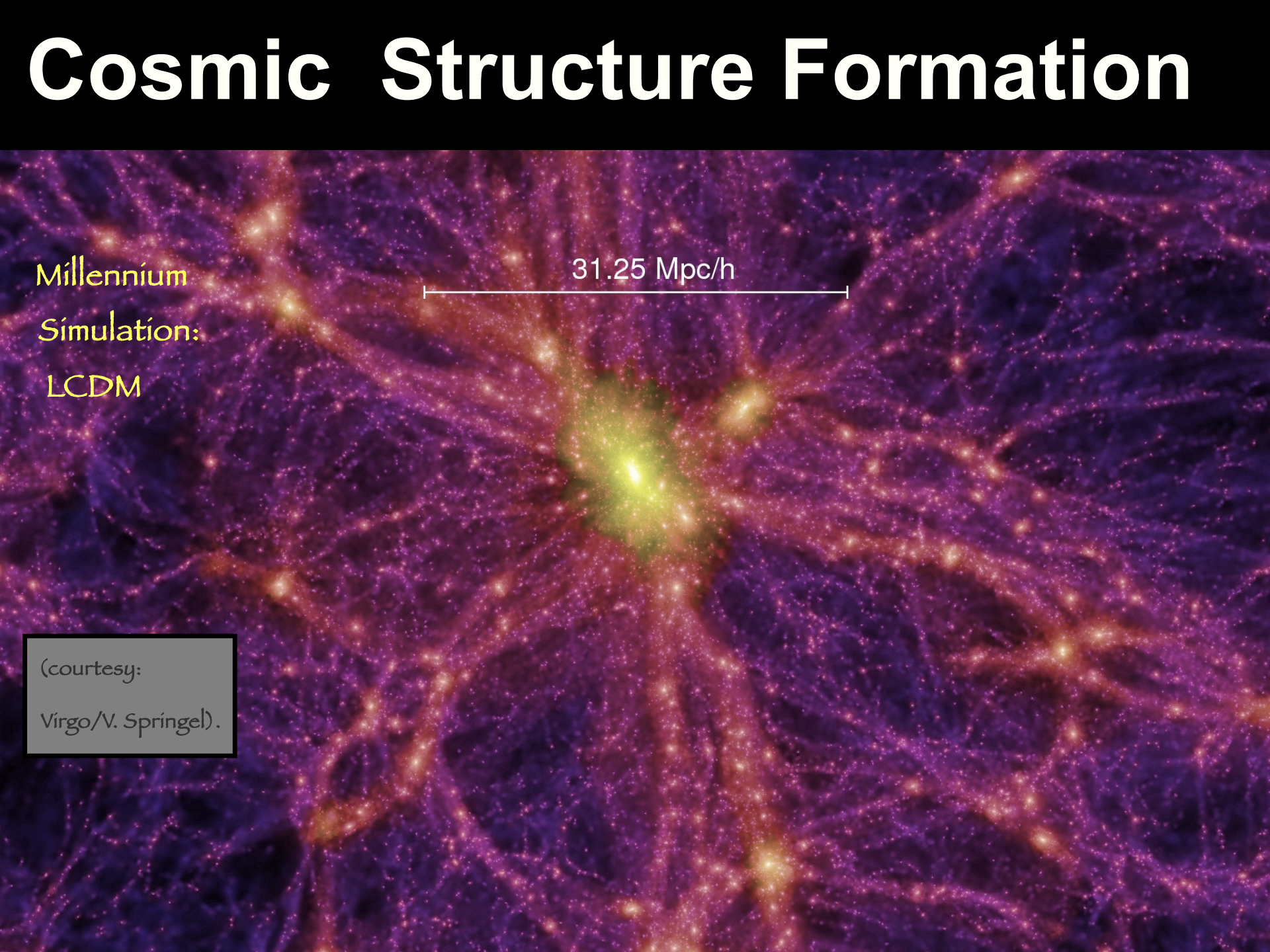
**without: not enough time
to form structure in the
Universe in 13.8 Gyrs**

**(cosmic web, clusters,
galaxies, stars, ...)**

Cosmic Structure Formation

Millennium
Simulation:
LCDM

31.25 Mpc/h



(courtesy:
Virgo/V. Springel).

Cosmic Structure Formation

**Formation
Cosmic Web:

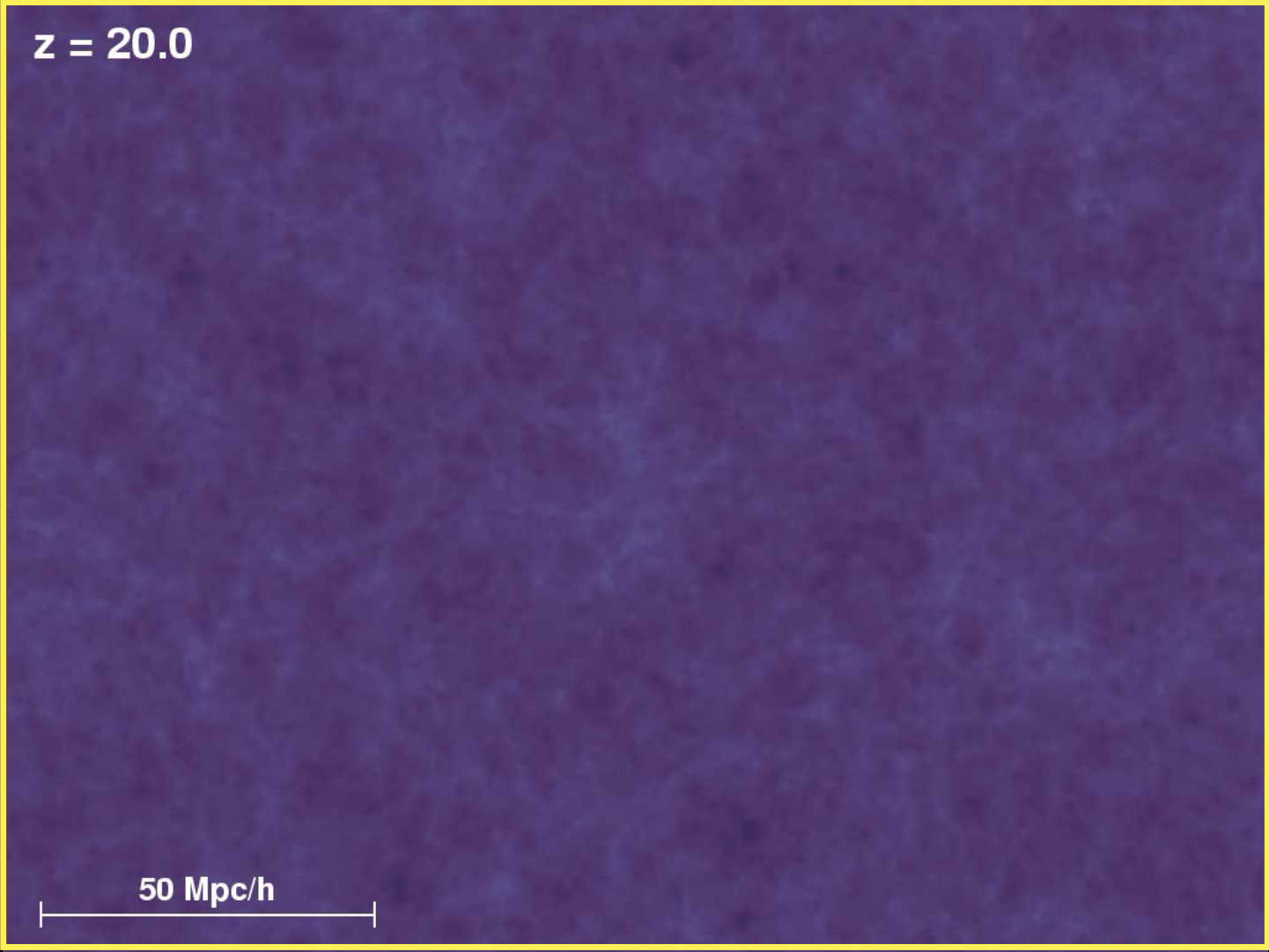
simulation
sequence

(cold)
dark matter**

(courtesy:
Virgo/V. Springel).

$z = 20.0$

50 Mpc/h

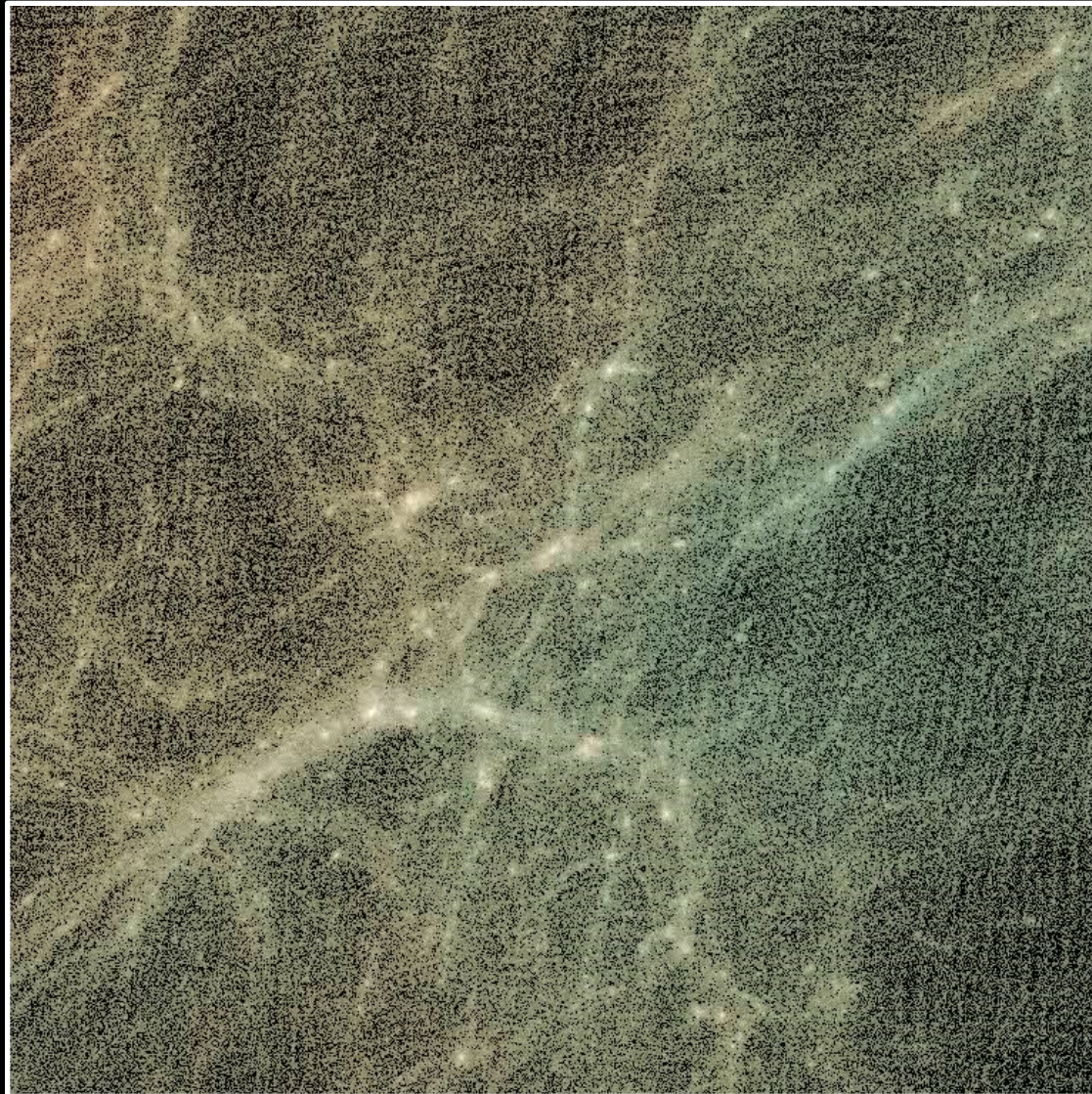
A large rectangular area filled with a dense, complex network of blue and purple filaments and nodes, representing the cosmic web at a high redshift. The structure is highly irregular and interconnected, with many small, bright spots (nodes) and long, thin lines (filaments) extending across the field of view. The overall color palette is dominated by deep blues and purples, with some lighter blue highlights.

Cosmic Web

Dynamical Evolution:

- Hierarchical buildup
- Tidally induced anisotropic evolution

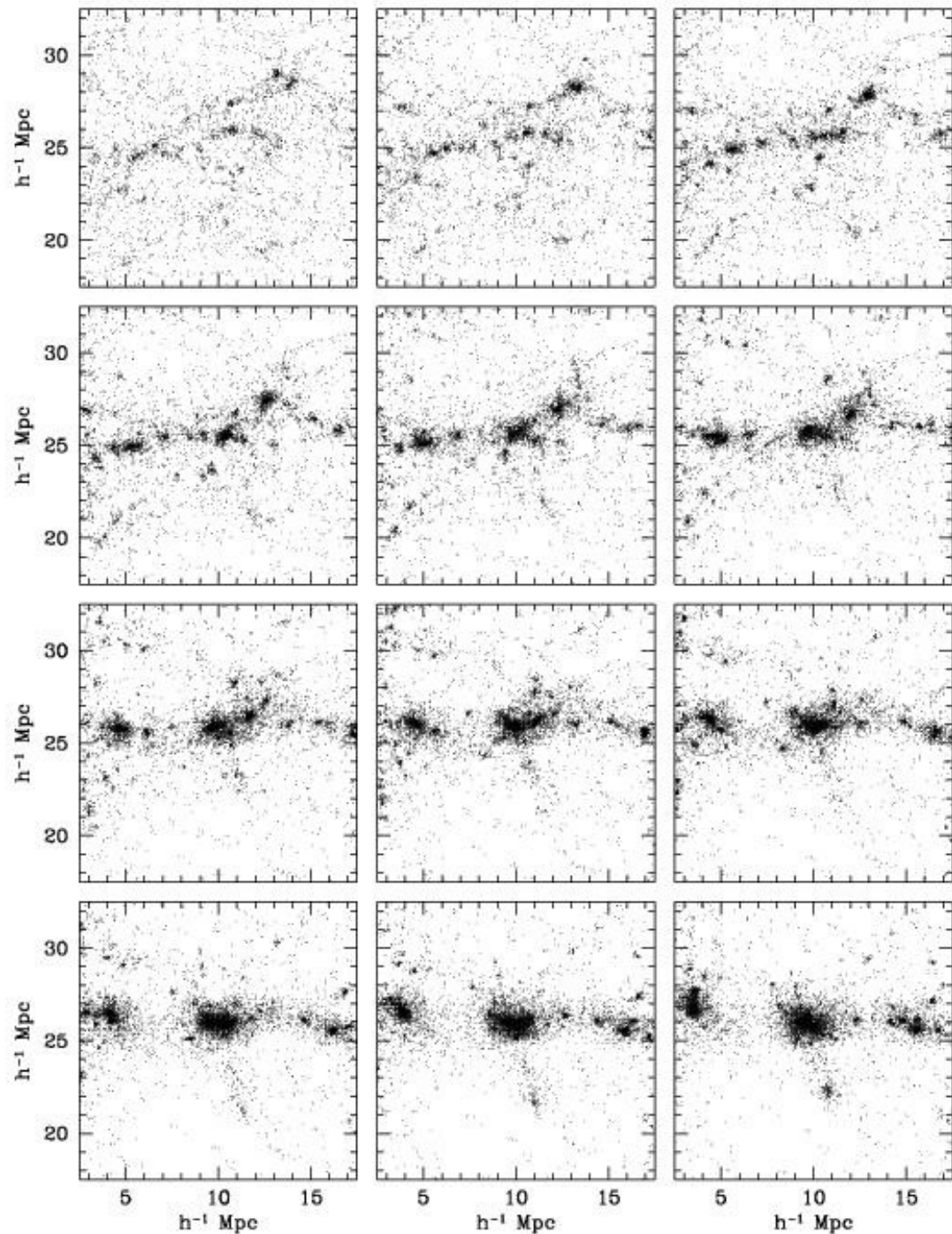
Hierarchical Evolution

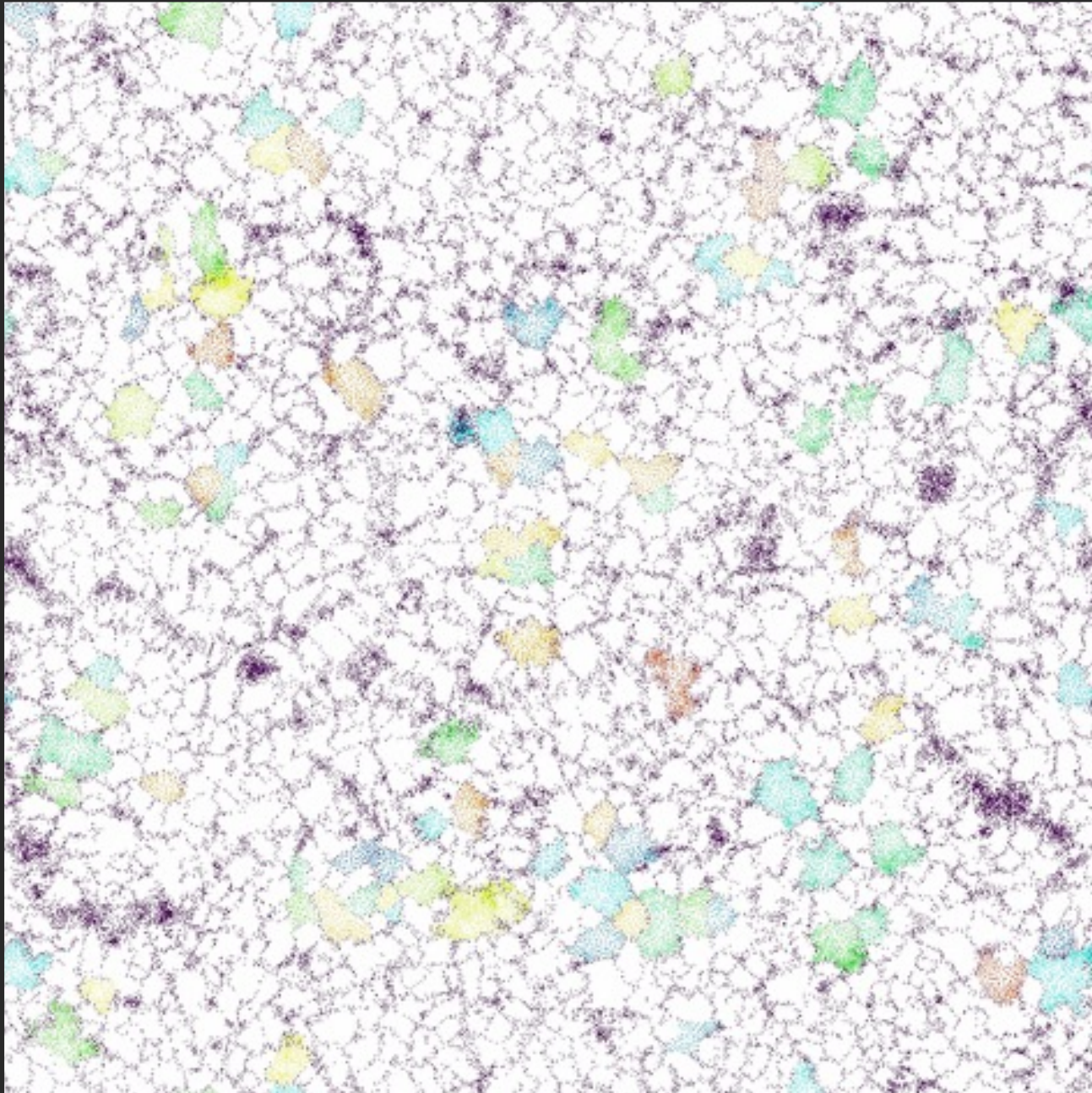


Rieder et al.
2013

**Structures in the Universe form
by
gradual hierarchical assembly:**

- ❖ small objects emerge & collapse first,
- ❖ then merge with other clumps
- ❖ while forming larger objects in hierarchy





Void Hierarchy:

“Lagrangian” view:

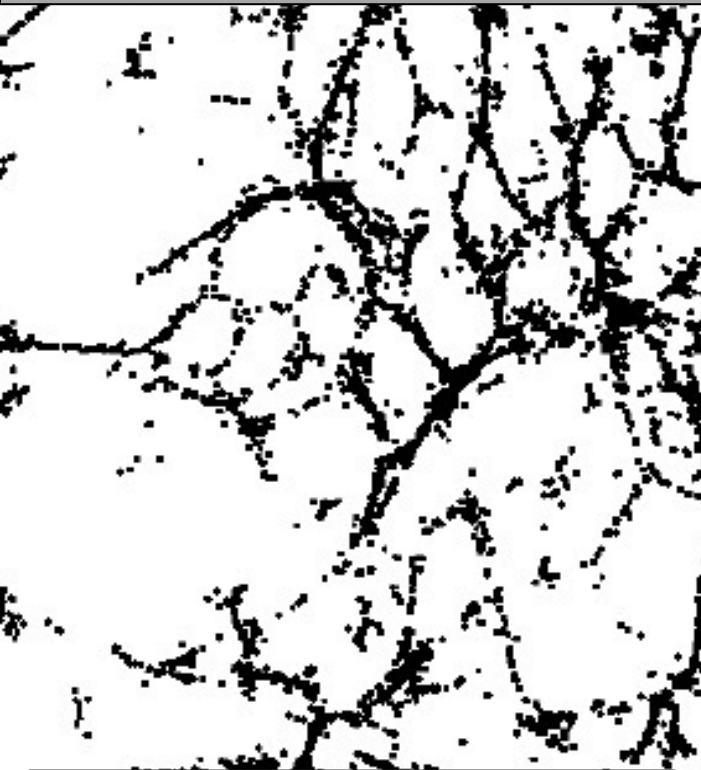
void-dominated
hierarchical
development
Cosmic Web

Platen & vdW 2004

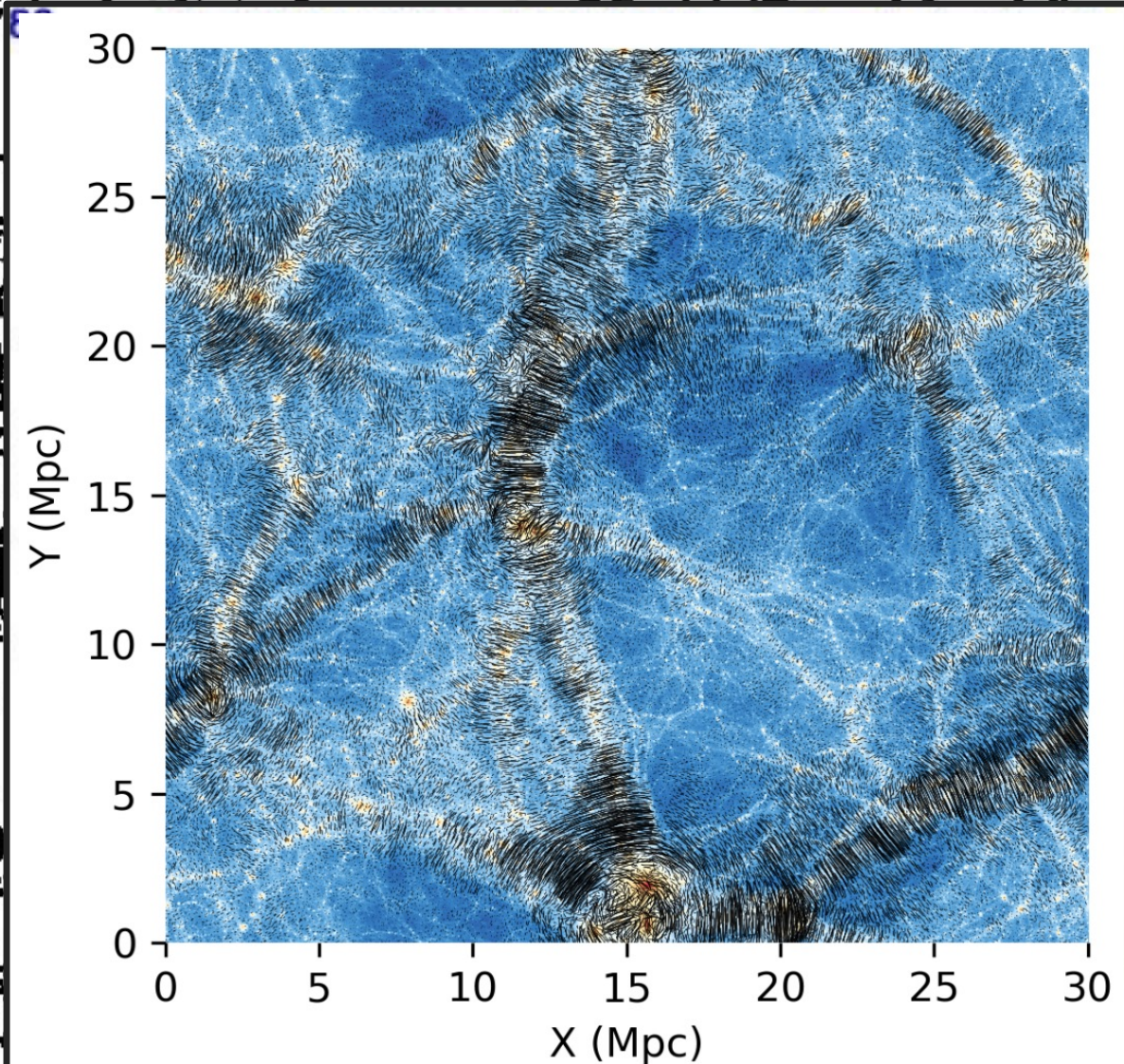
Sheth & vdW 2004

Aragon-Calvo &
Szalay 2012

Tidal Shaping of the Cosmic Web



**Tidal Forces
shape the Cosmic Web**

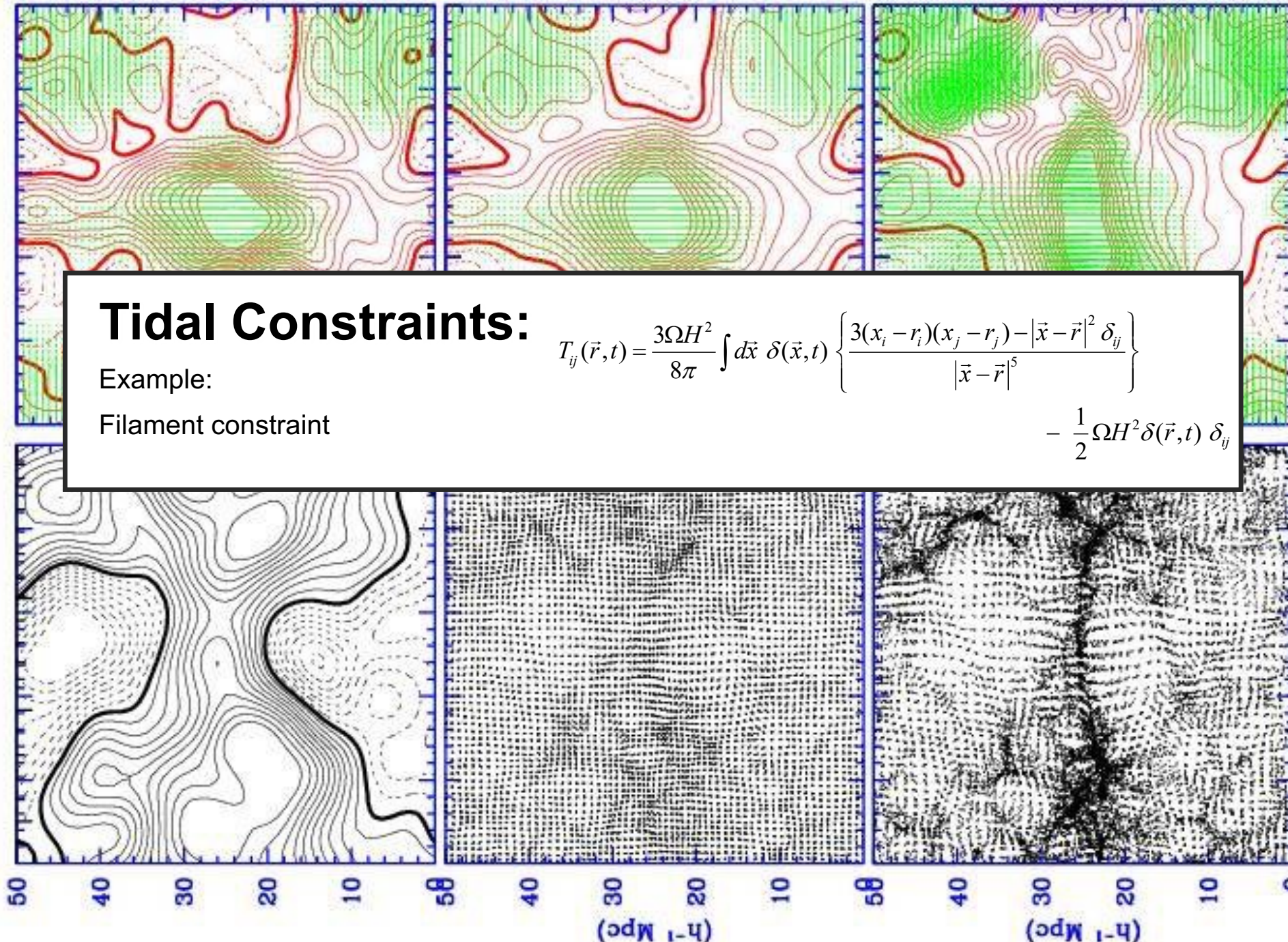


Tidal Constraints:

Example:

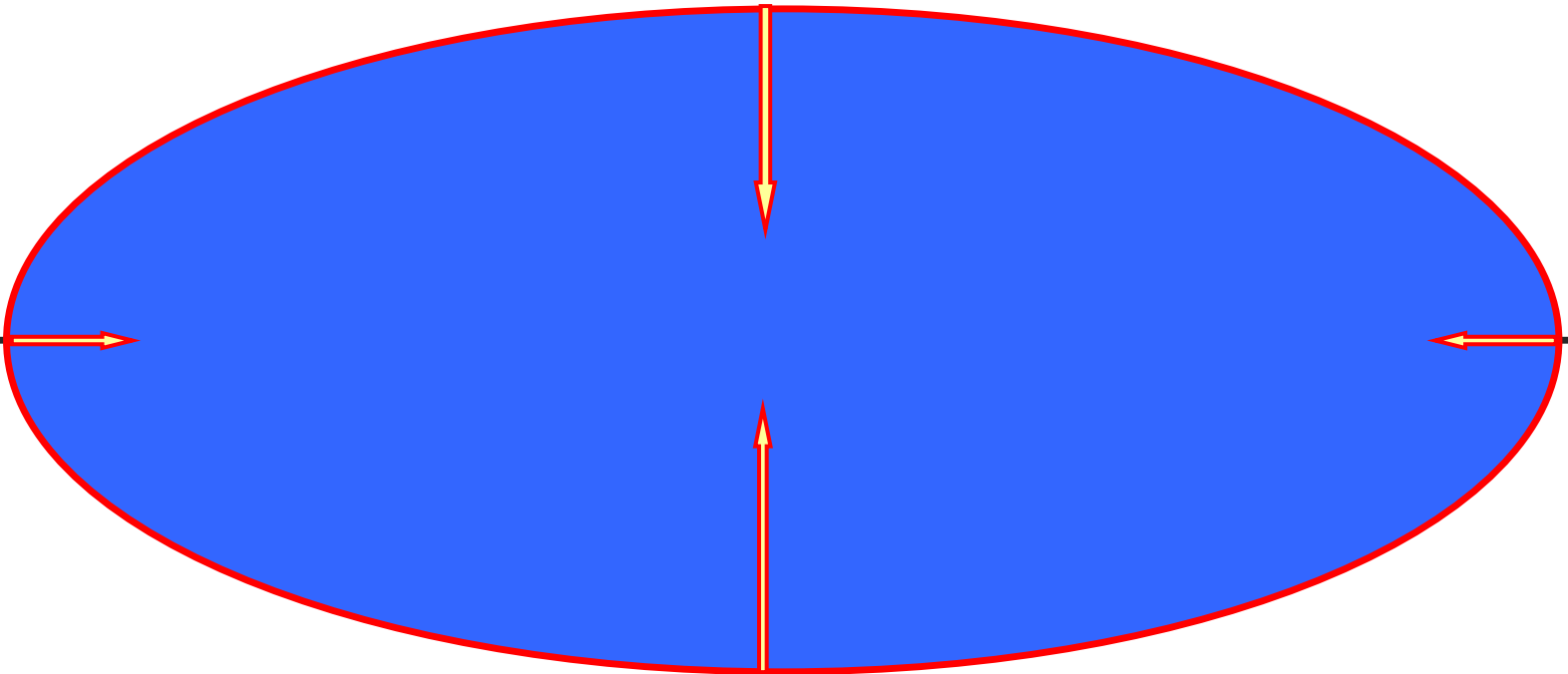
Filament constraint

$$T_{ij}(\vec{r}, t) = \frac{3\Omega H^2}{8\pi} \int d\vec{x} \delta(\vec{x}, t) \left\{ \frac{3(x_i - r_i)(x_j - r_j) - |\vec{x} - \vec{r}|^2 \delta_{ij}}{|\vec{x} - \vec{r}|^5} \right\} - \frac{1}{2} \Omega H^2 \delta(\vec{r}, t) \delta_{ij}$$



Anisotropic Gravitational Collapse

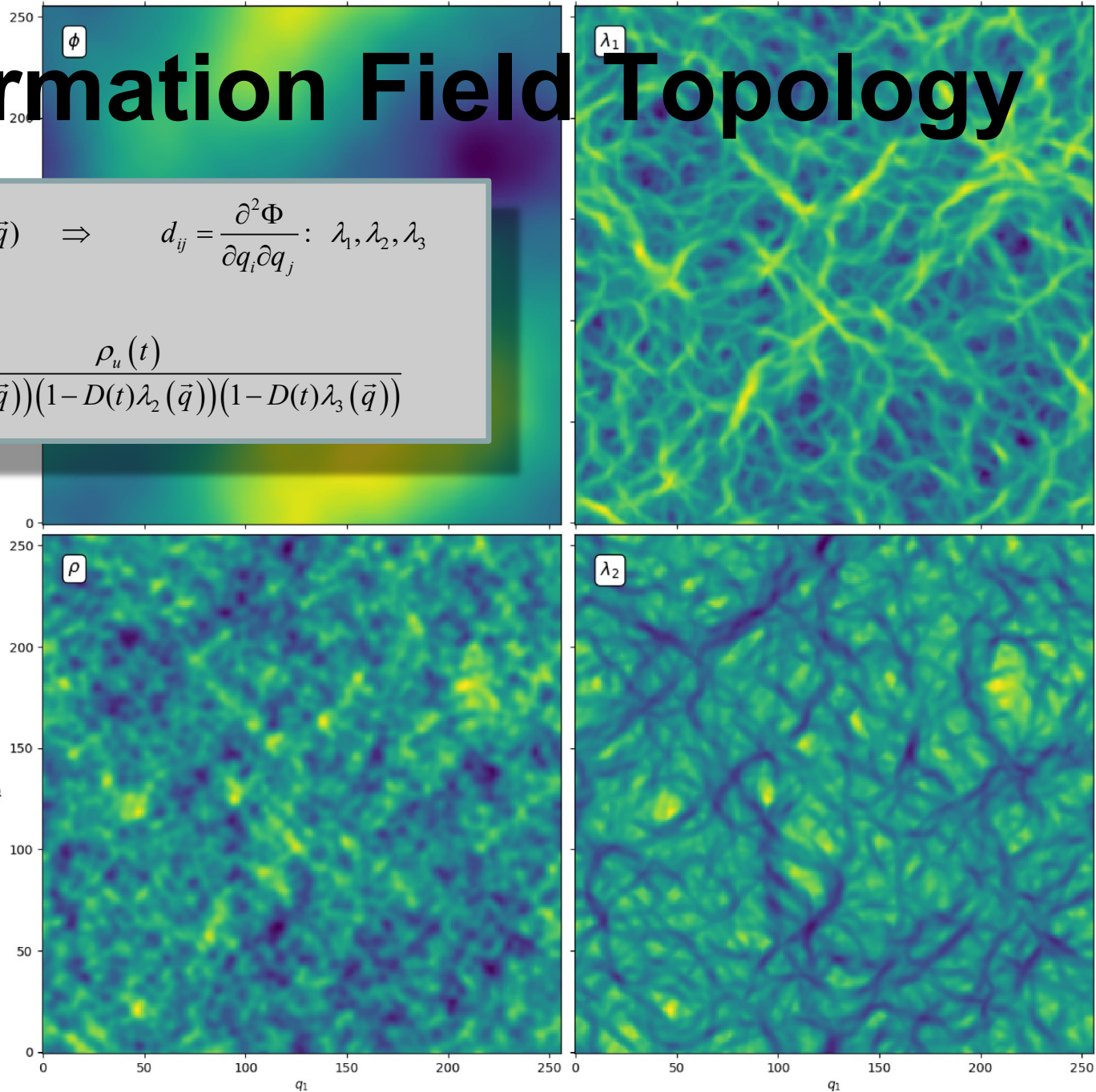
Amplification
small perturbations in gravity along different directions (tidal forces)



Deformation Field Topology

$$\vec{x}(\vec{q}, t) = \vec{q} - D(t) \vec{\nabla} \Phi(\vec{q}) \quad \Rightarrow \quad d_{ij} = \frac{\partial^2 \Phi}{\partial q_i \partial q_j} : \lambda_1, \lambda_2, \lambda_3$$

$$\rho(\vec{q}, t) = \frac{\rho_u(t)}{(1 - D(t)\lambda_1(\vec{q}))(1 - D(t)\lambda_2(\vec{q}))(1 - D(t)\lambda_3(\vec{q}))}$$



**Deformation eigenvalue
Landscape**
(initial Gaussian field)

**Connectivity
Cosmic Web:**

**Topology
deformation field**

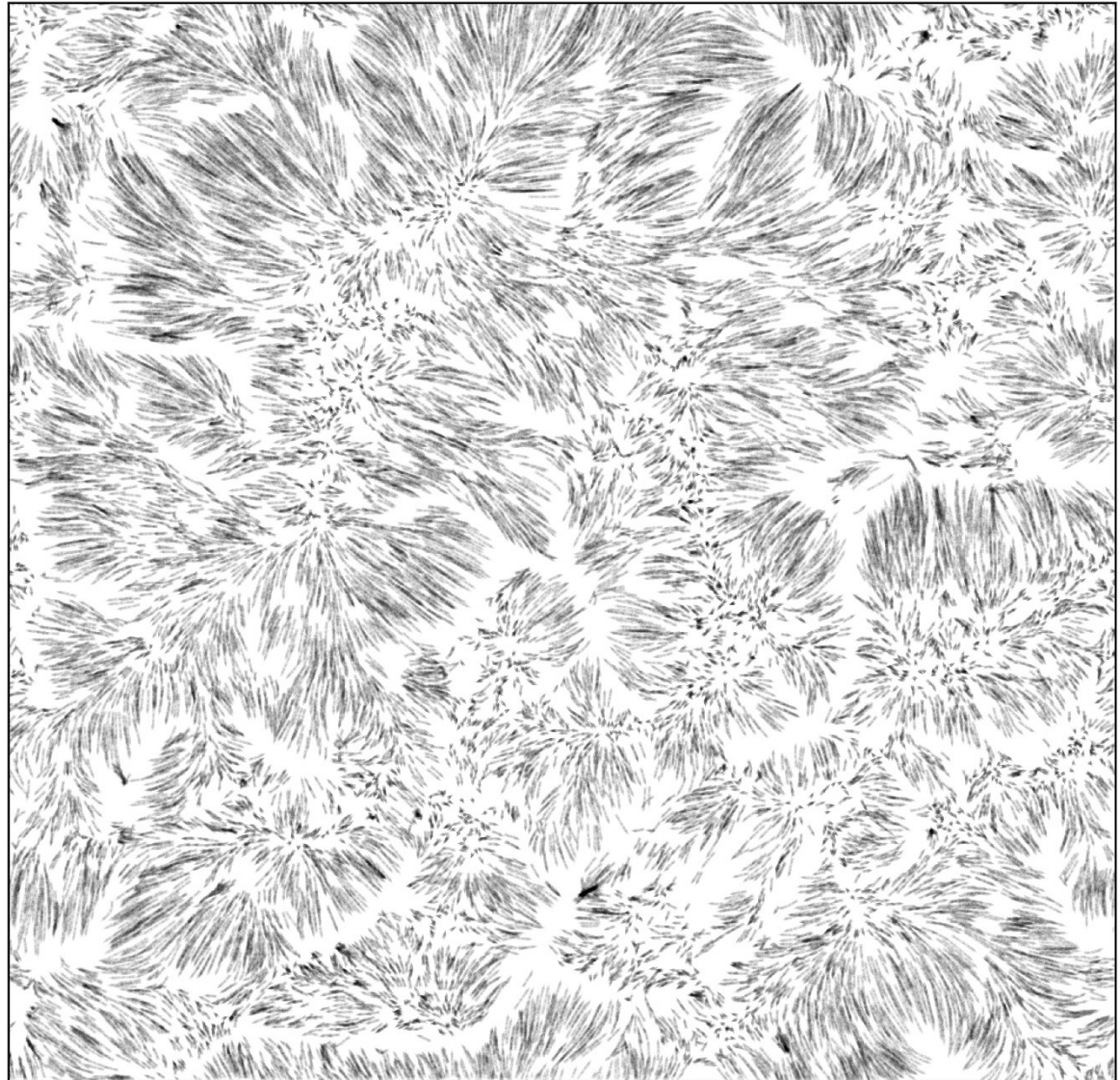
Cosmic Web Dynamics: Summary

- *Filaments rule!*

yet

- *Voids organize!*

- strict hierarchy
filaments-voids-walls-cluster nodes
- Filaments dominate force & tidal field
- Voids organize:
 - structural pattern cosmic web
 - connectivity cosmic web
- Voids very important at high z
- Cluster nodes:
relatively recent & fast
growing influence



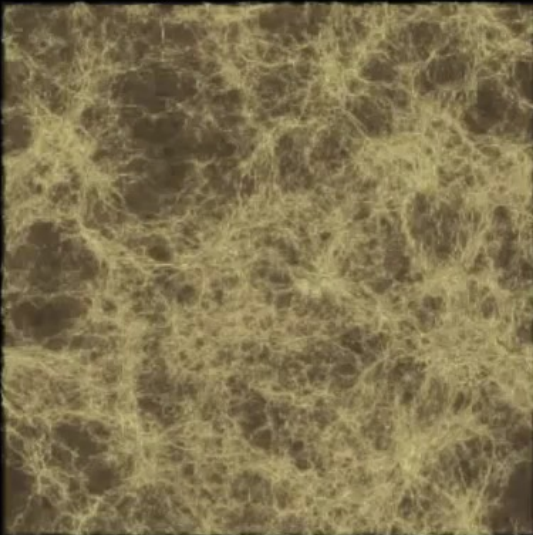
the Cosmic Web:

**evolution of
walls & filaments**

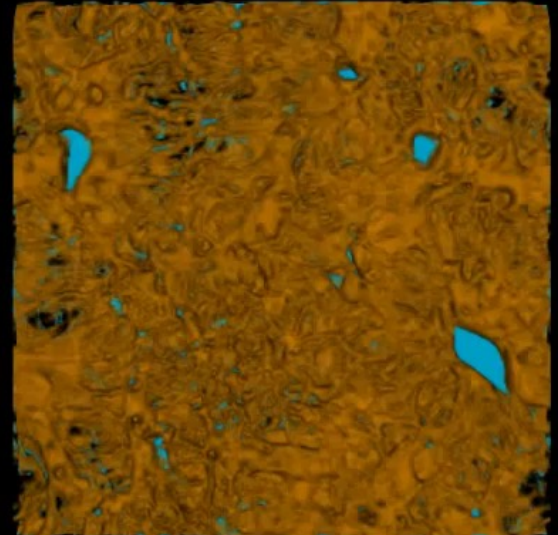
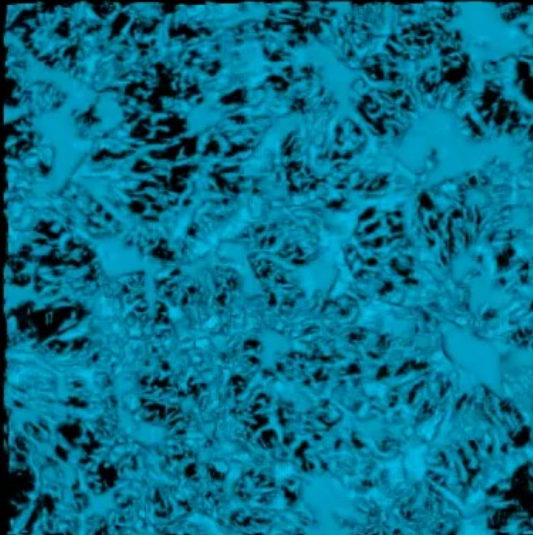
NEXUS/MMF

Evolution Cosmic Web

$t = 0.56$ Gyrs



$z = 8.70$



CGV:

on walls & filaments

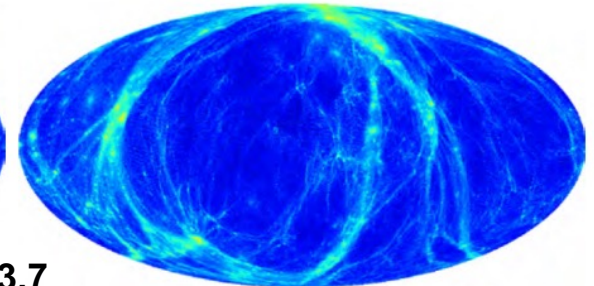
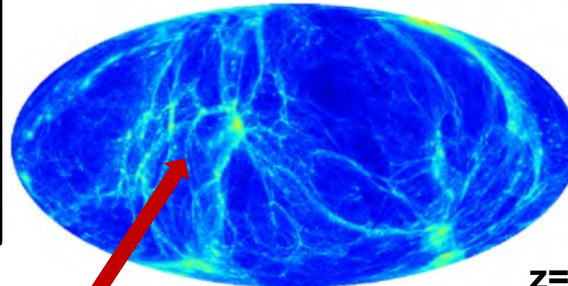
- Mollweide sky projection matter distribution around CGV halos
- CGV halos embedded in walls
- Walls dominate void infrastructure
- substantial fraction in filaments (embedded in walls)
- active dynamical evolution of wall-filament goes along with active void galaxy halo evolution

merging system of
Intravoids walls

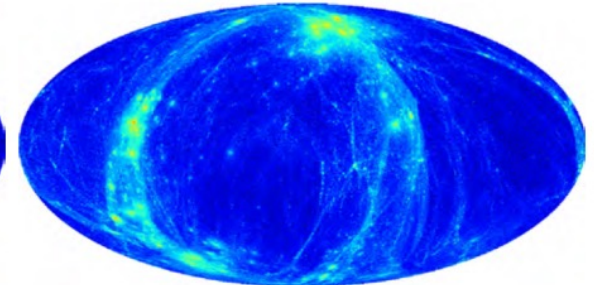
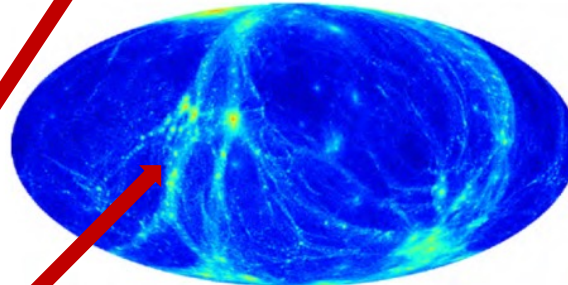
Rieder et al. 2013

CGV_D

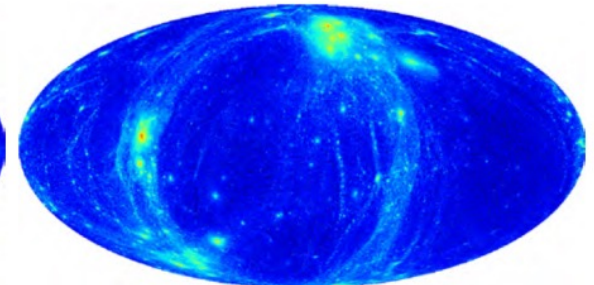
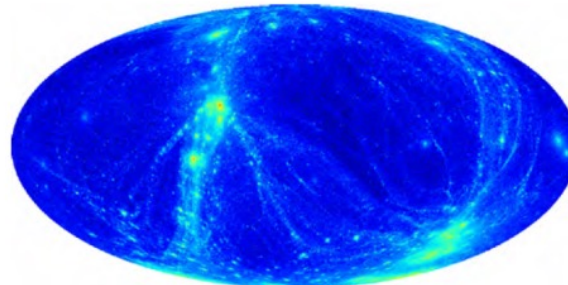
CGV_G



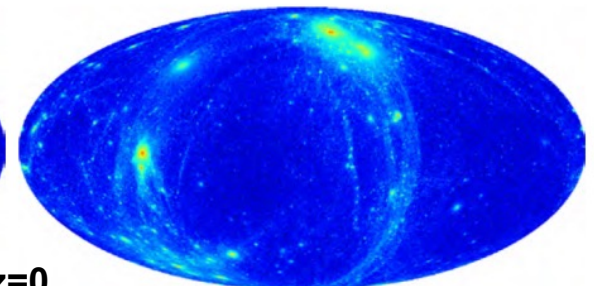
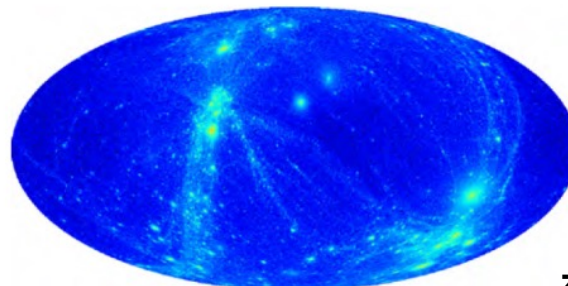
$z=3.7$



$z=1.6$

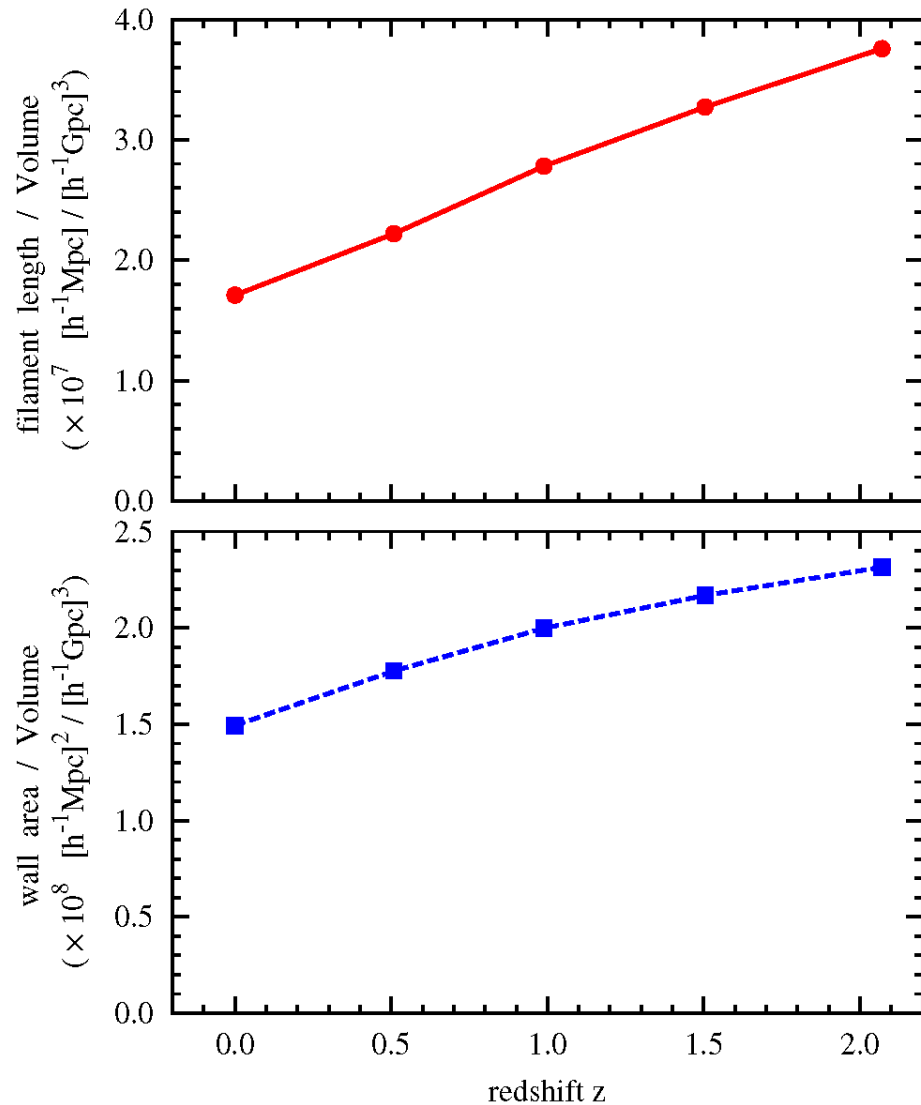


$z=0.55$



$z=0$

Evolving Filament & Wall Network

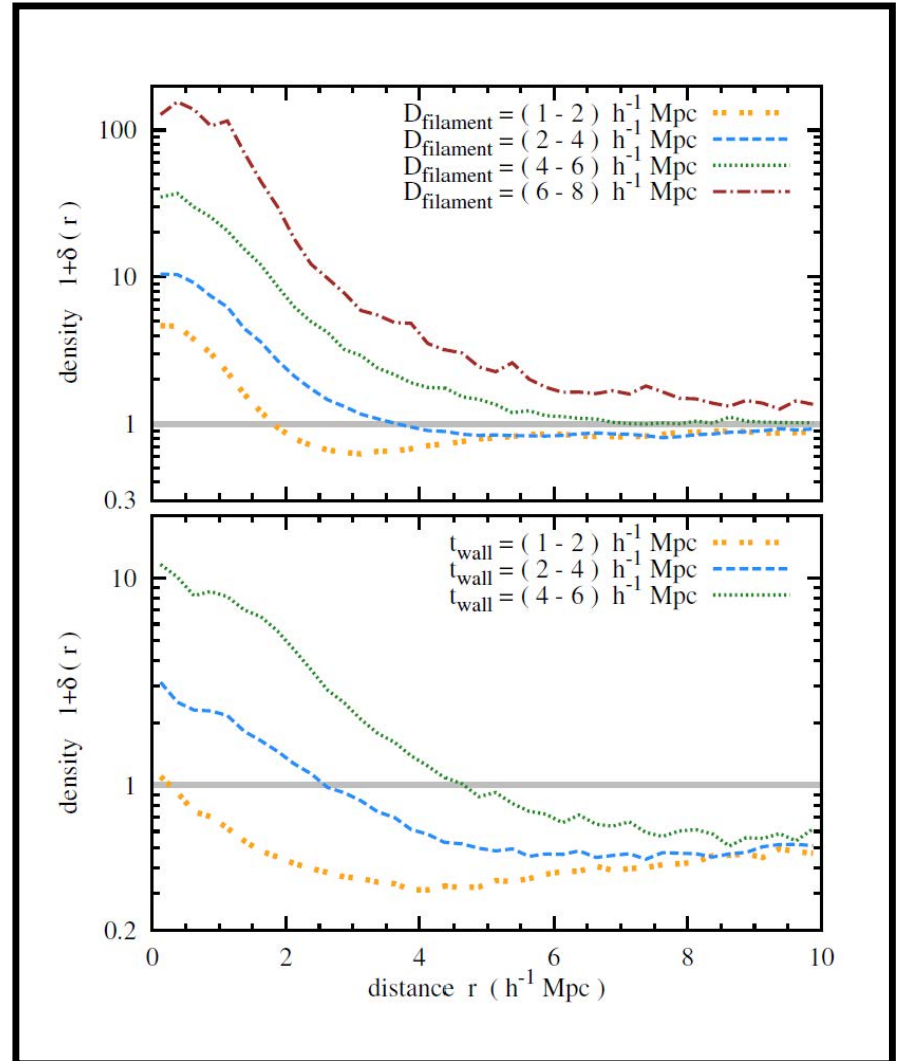
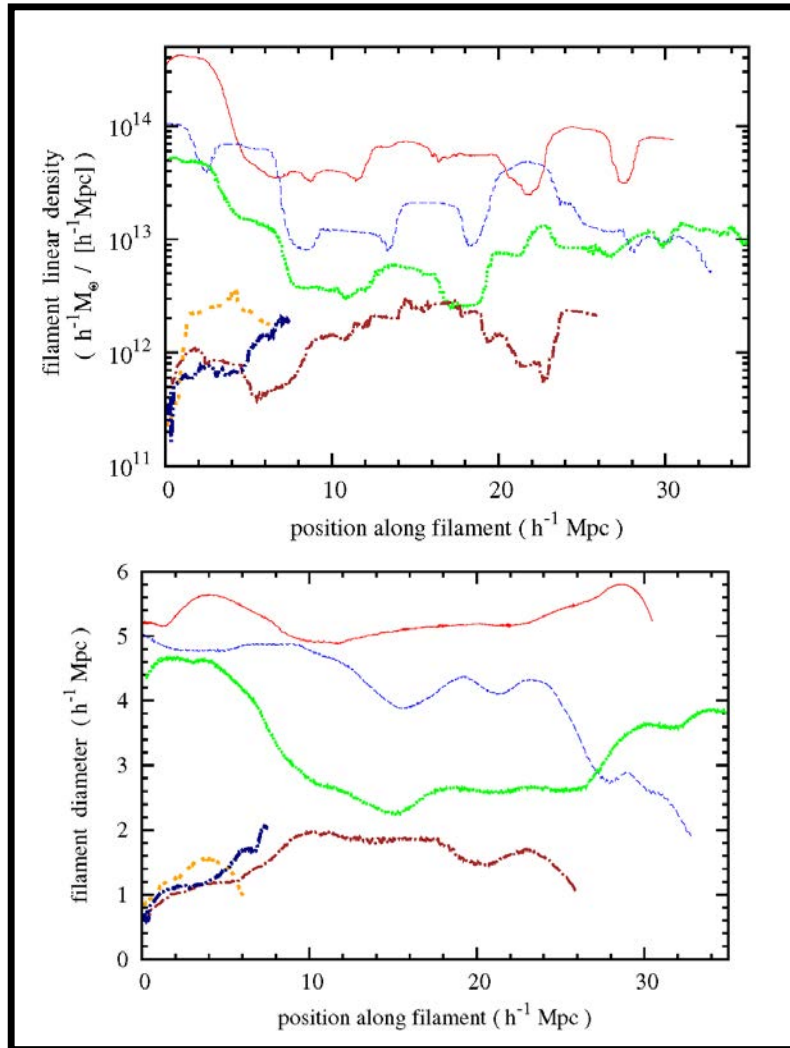


Total length of filament network :
decreasing as a function of time

Total surface area of wall network :
decreasing as a function of time

Walls & Filaments

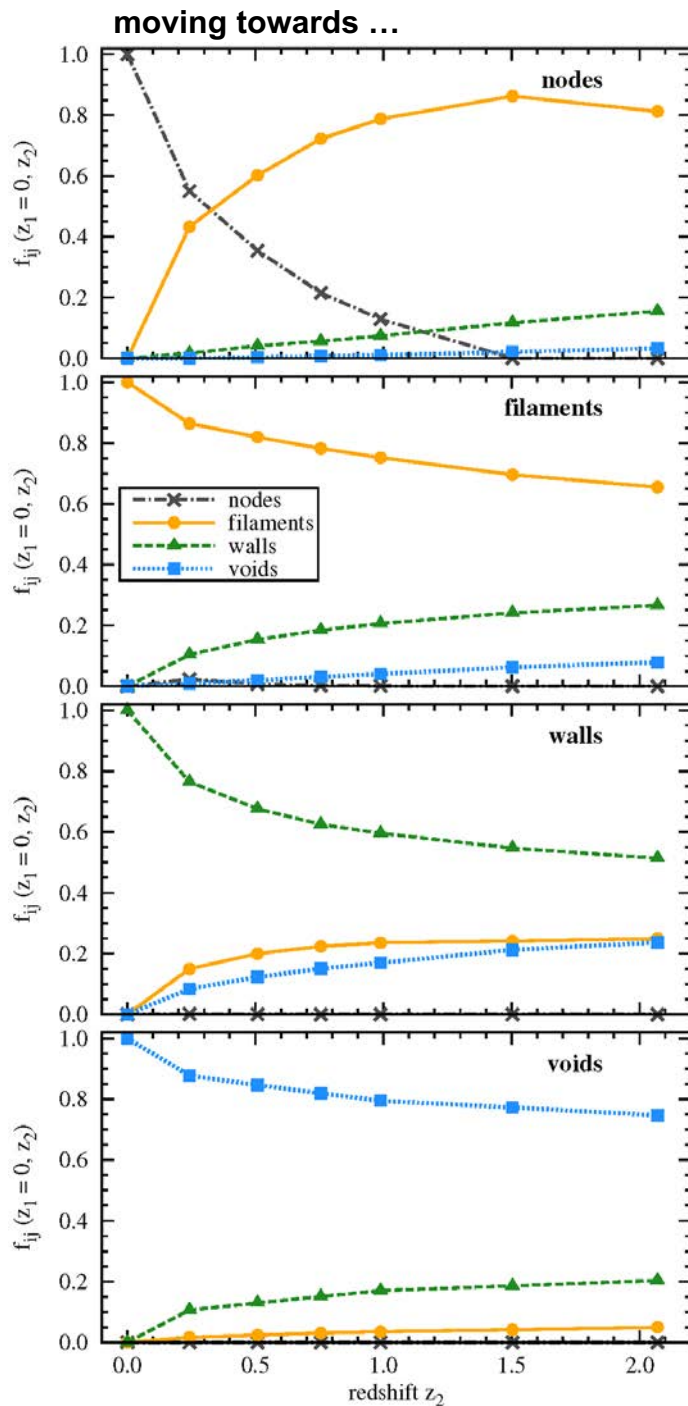
Internal Diameter & Density Profiles



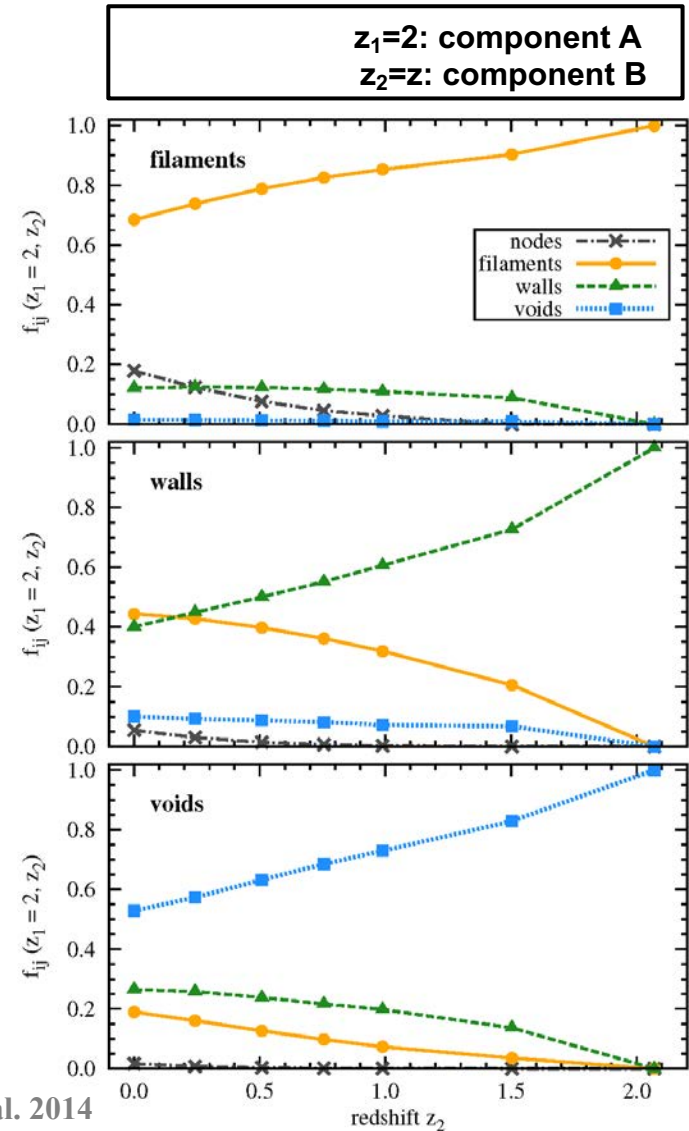
Cosmic Web:

Evolutionary Trends

Web Migration



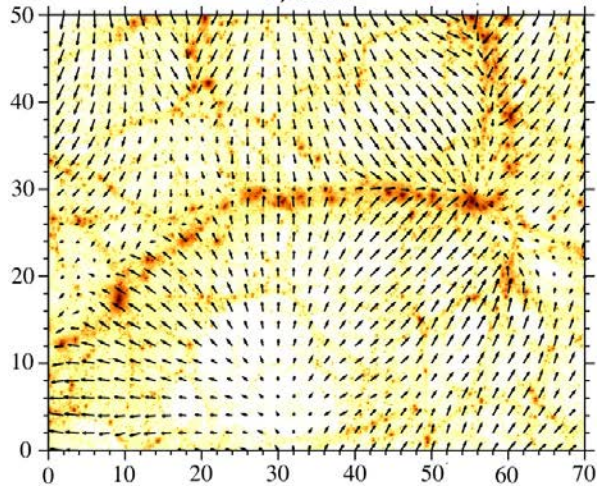
$z_1=0$: component B
 $z_2=z$: component A



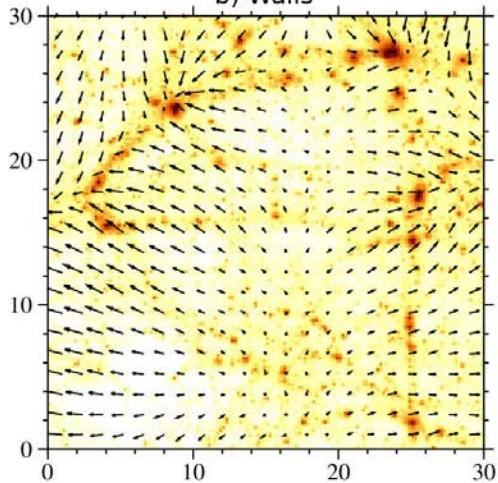
$z_1=2$: component A
 $z_2=z$: component B

Web Mass Emigration

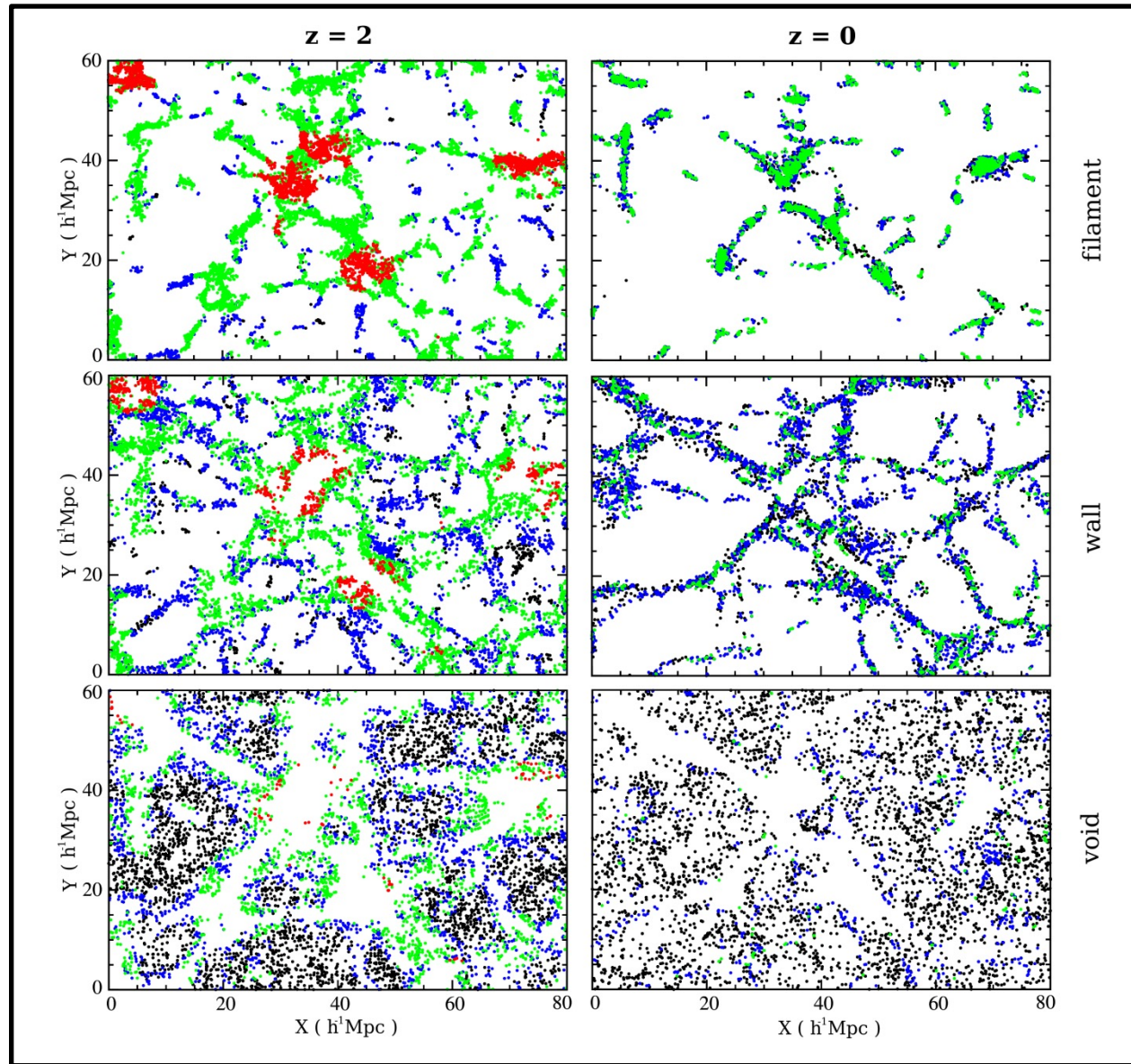
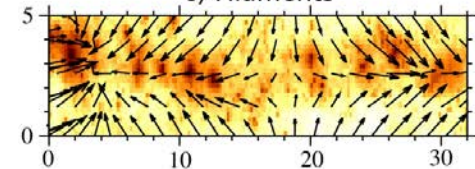
a) Voids



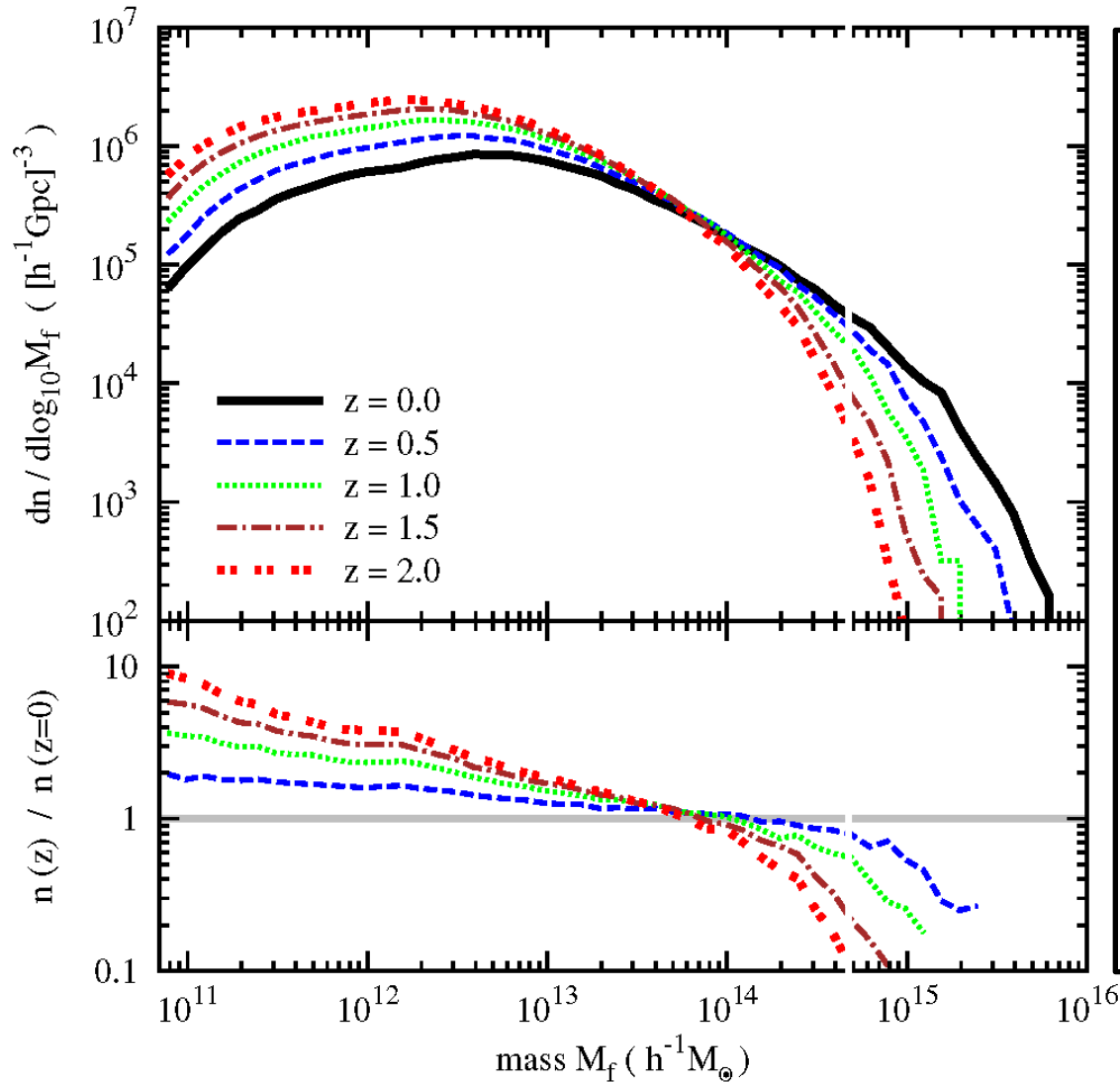
b) Walls



c) Filaments



Evolving Filament Population



Filament Mass Function:

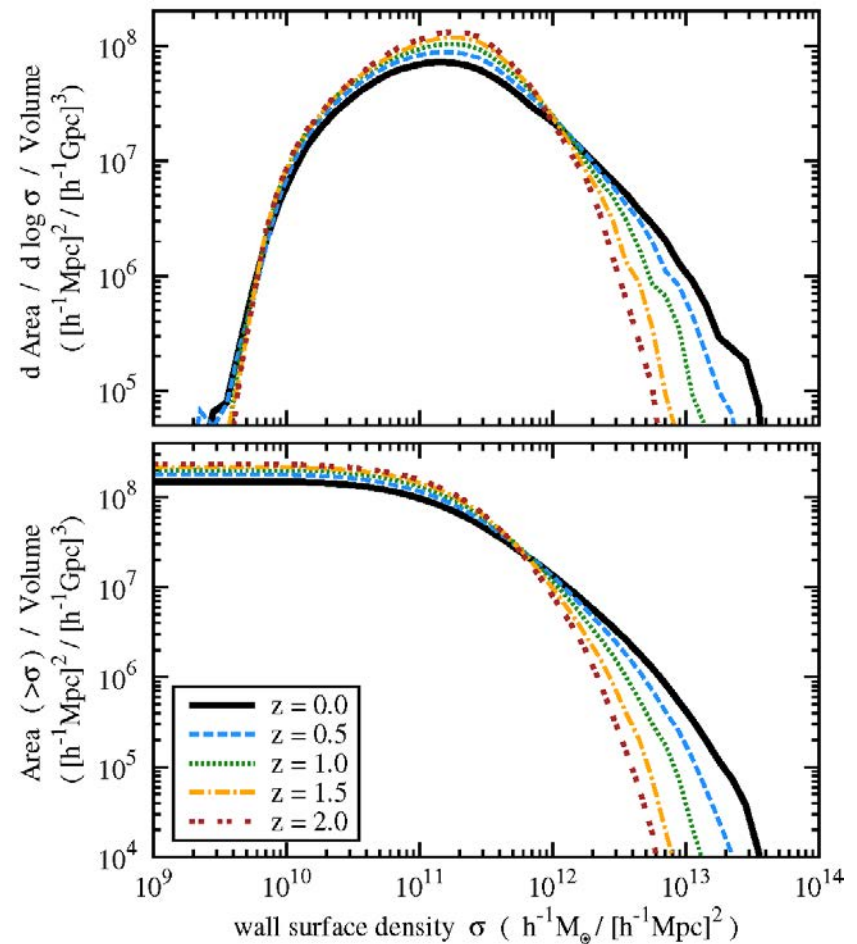
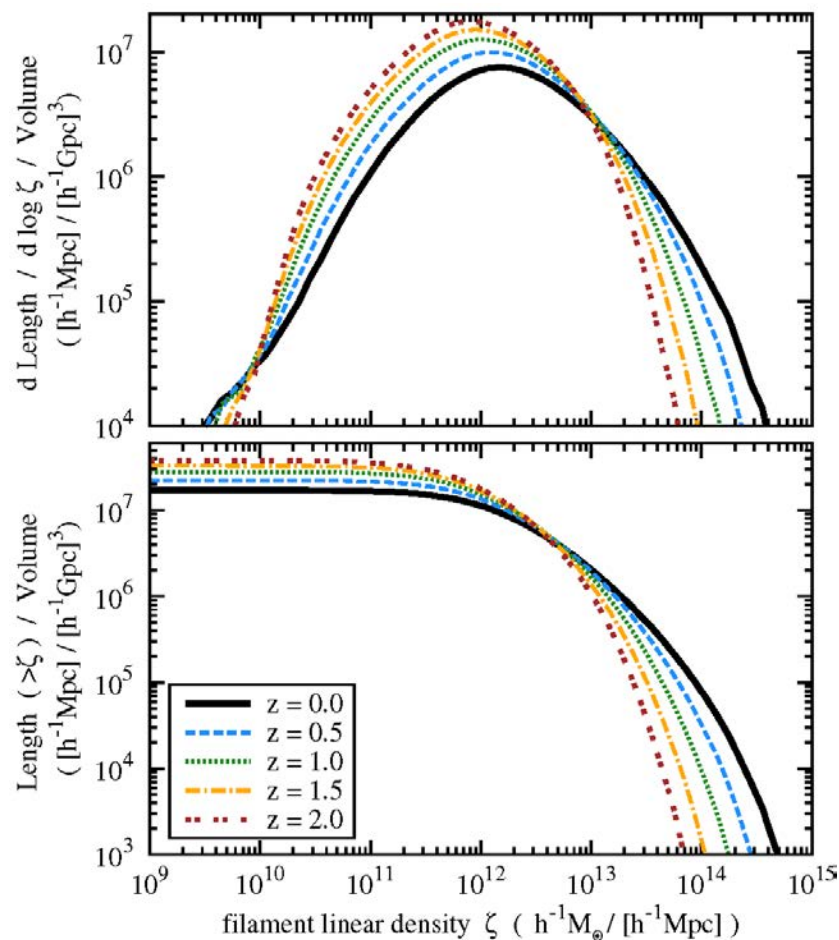
- shifting from small to large mass filaments
- reflection hierarchical evolution filament population

Evolving Filament & Wall Densities

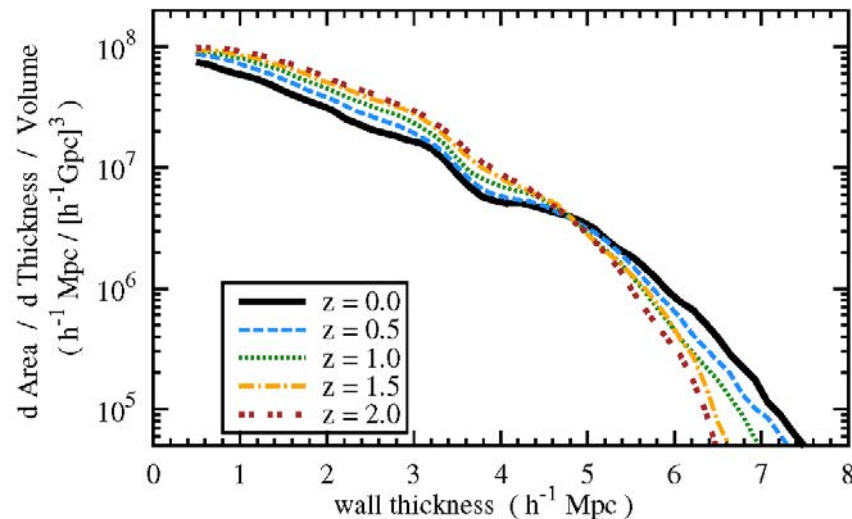
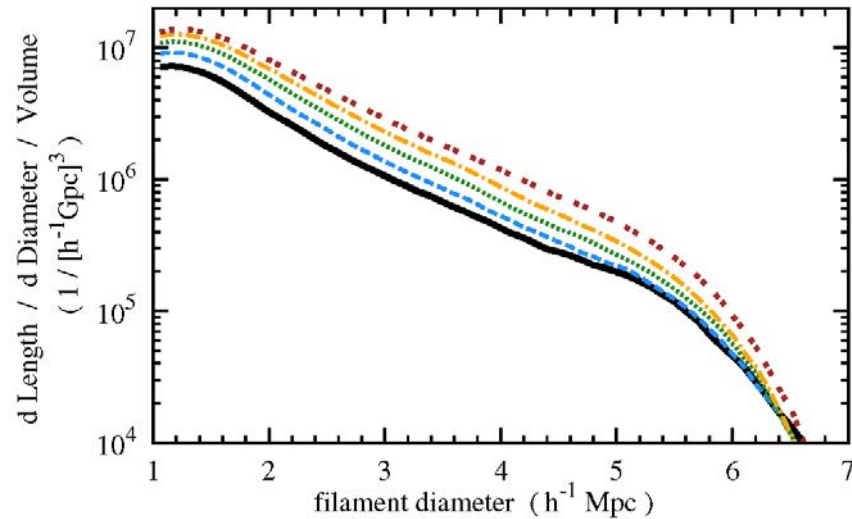
Filament population: evolves continuously towards more dense filaments

Wall population: tenuous walls do not evolve into more dense walls

Cautun et al. 2014



Evolving Filament & Wall Diameters



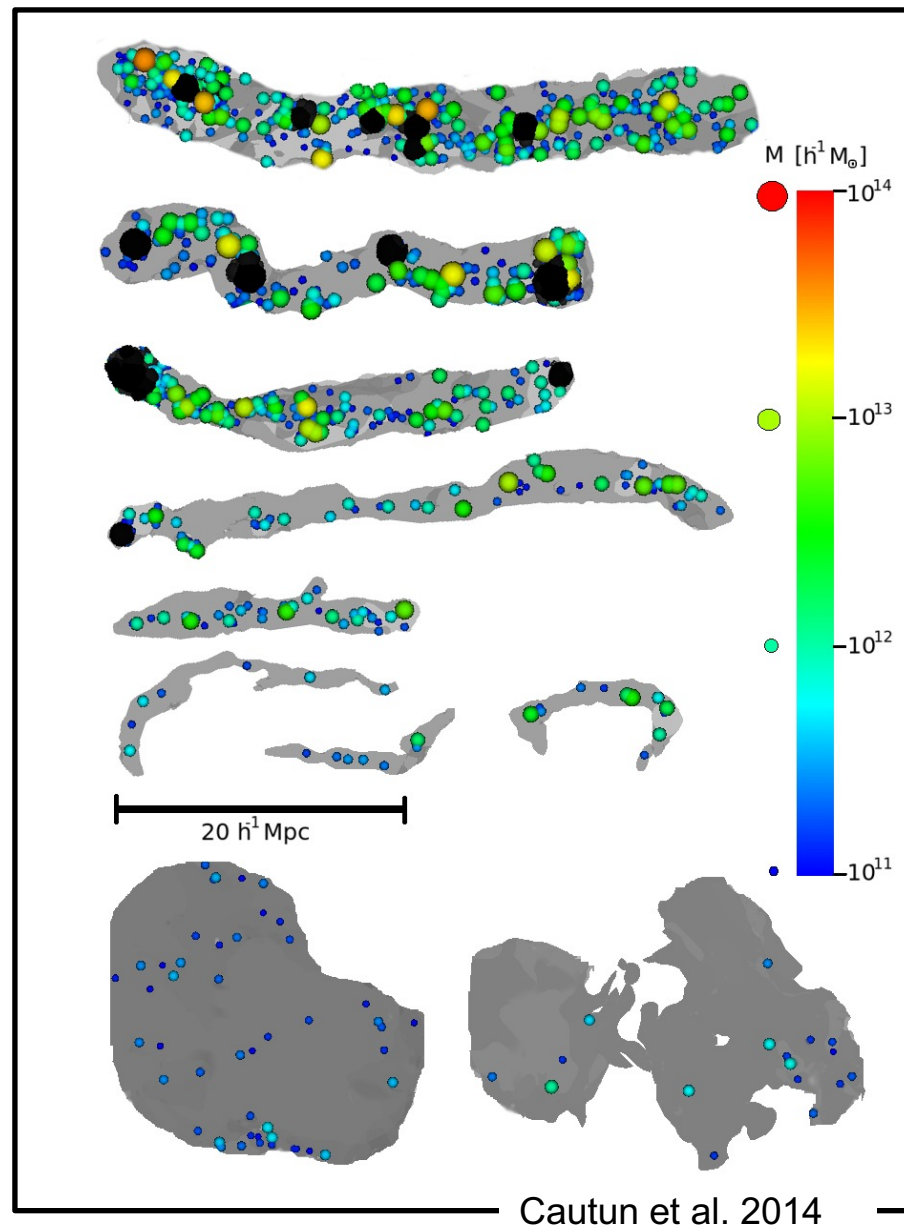
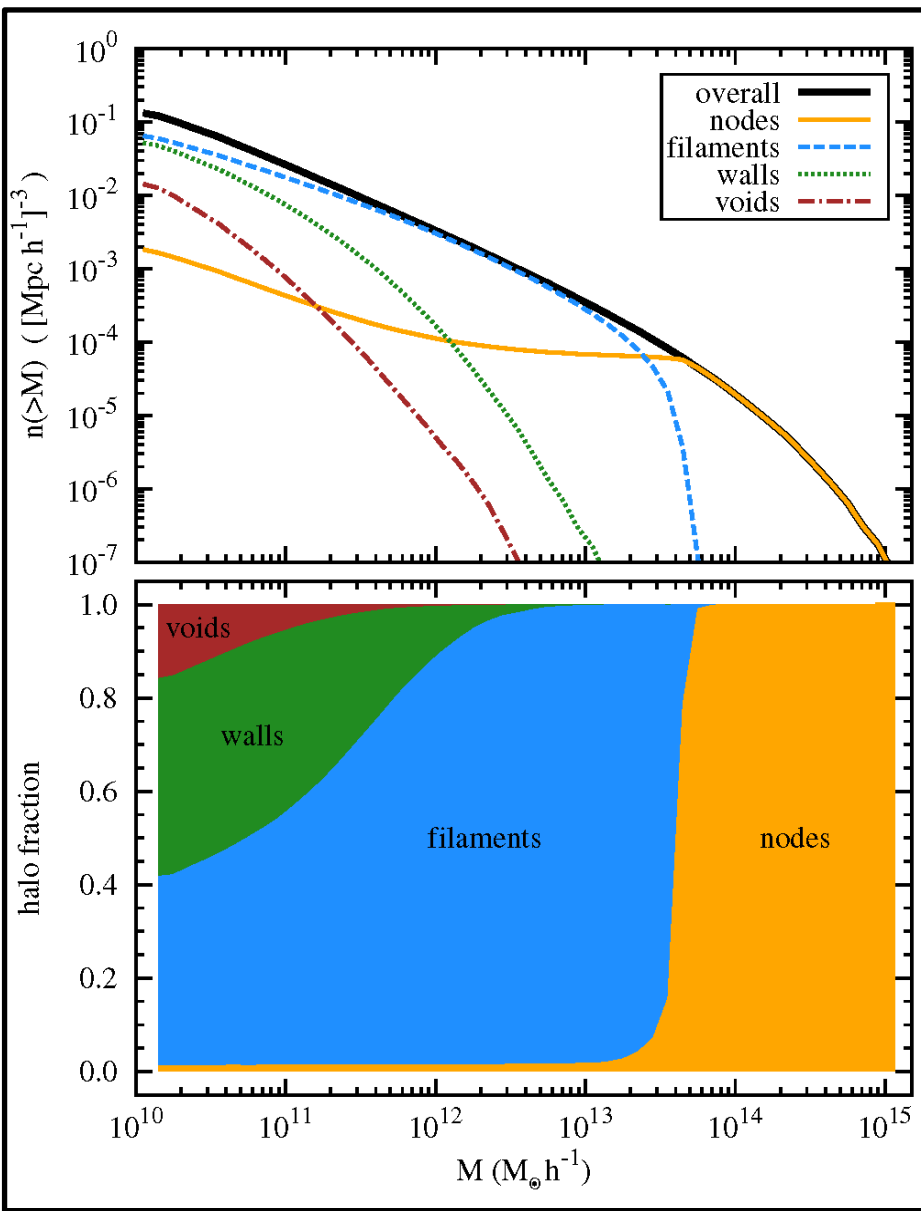
Filament population:
increasing diameter

Wall population:
increasing thickness for denser walls
decrease of tenuous walls

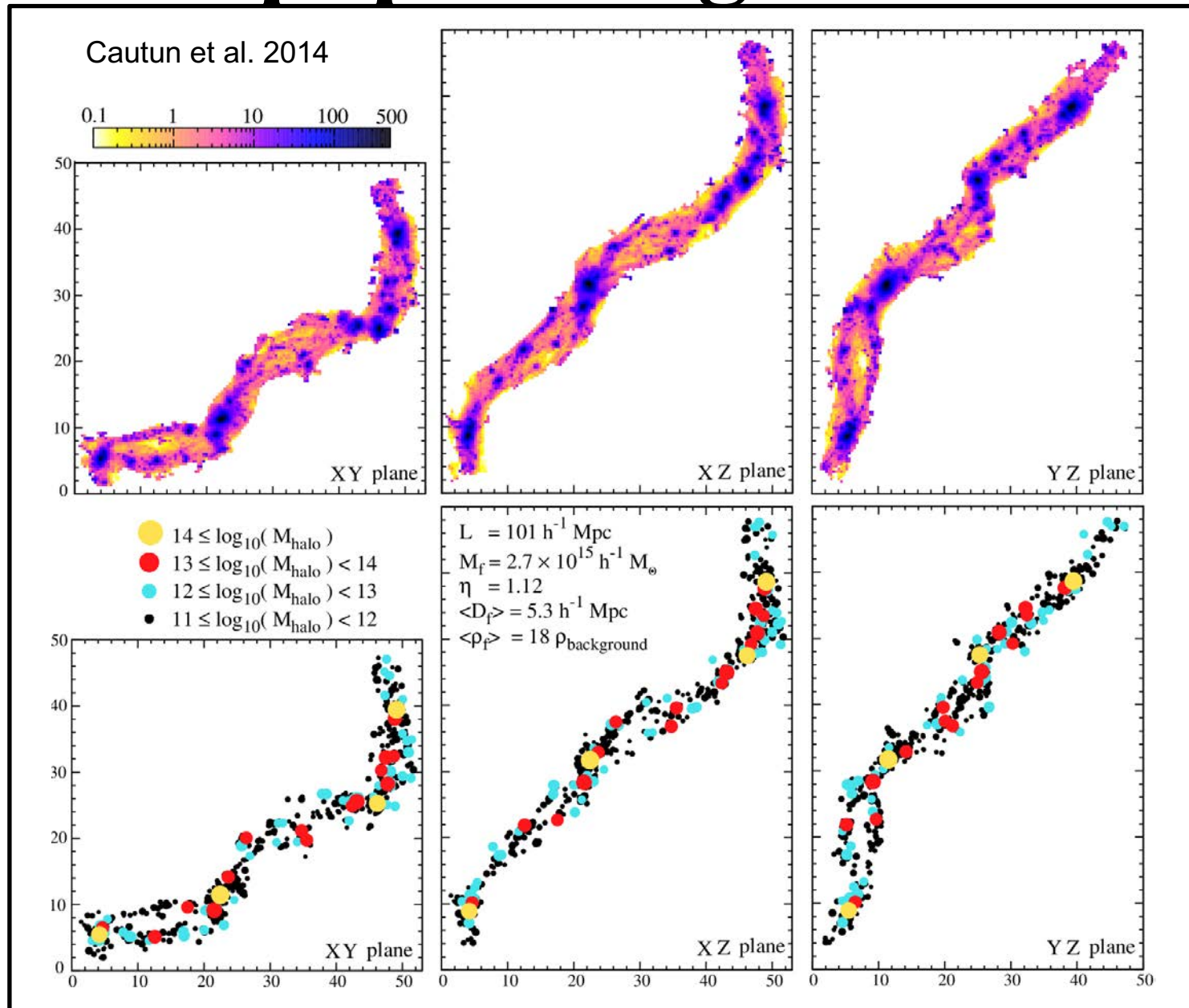
Cosmic Web:

Halo Distribution

Halos in the Cosmic Web



Halos populating Filaments

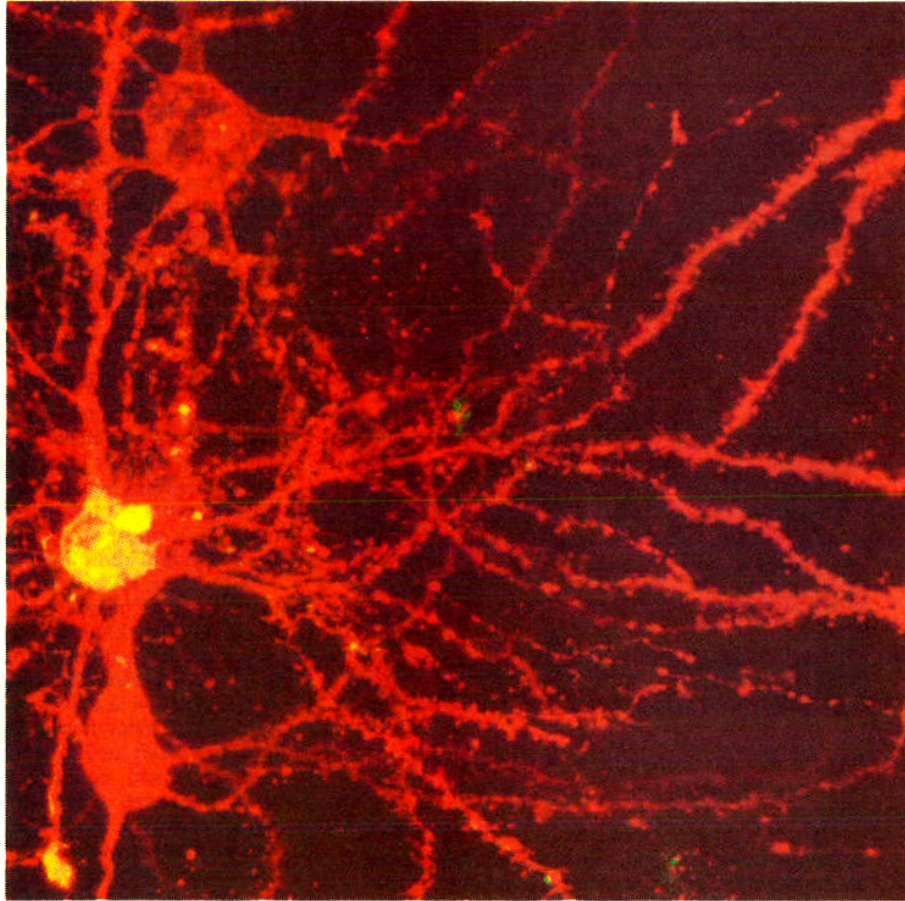


Objectives

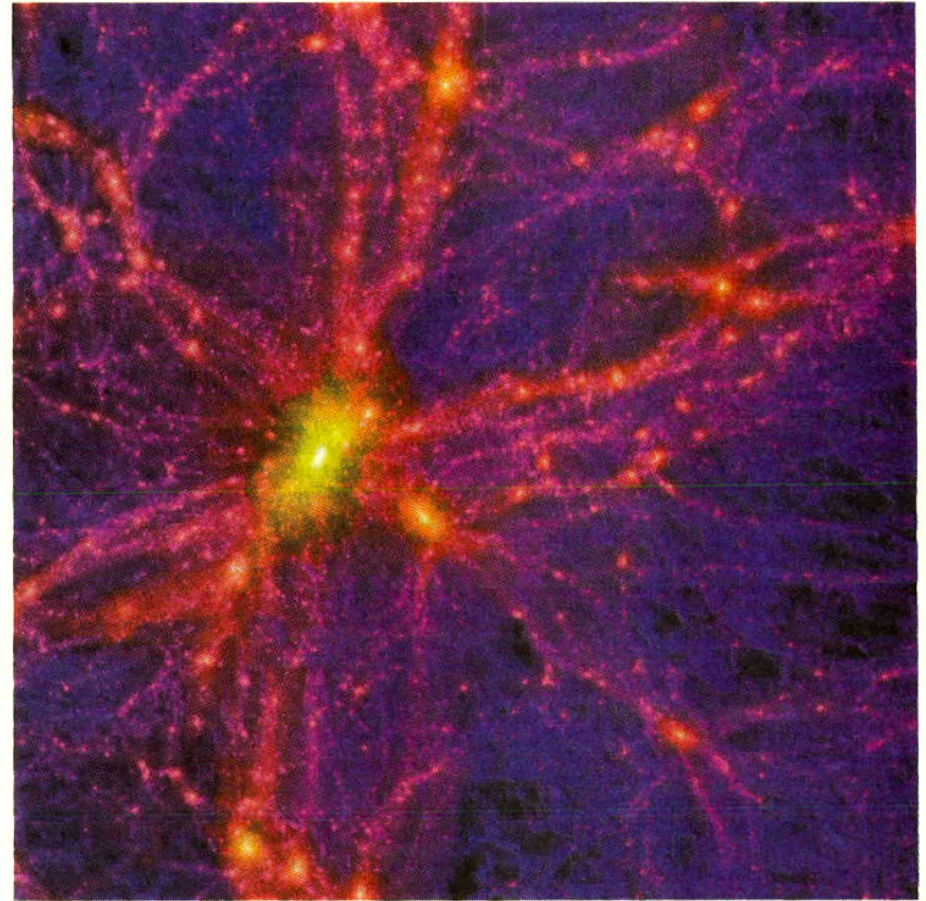
Complex macroscopic patterns in nature arise from the action of basic, often even simple, physical forces and processes. In many physical systems, the spatial organization of matter is one of the most readily observable manifestations of the nonlinear collective actions forming and moulding them.

The richly structured morphologies are a rich source of information on the physical forces at work and the conditions under which the systems evolved. In many branches of science the study of geometric patterns has therefore developed into a major industry for exploring and uncovering the underlying physics

Balbus & Hawley 1998



Mark Miller



Virgo Consortium

Scientific Themes:

- L'art pour l'art:
 - The cosmic web is an interesting astrophysical structure, of intriguing complexity & geometry
 - challenge to understand its structure & dynamics
 - “and the forces & processes that shaped it ...”
- Cosmology:
 - Is there cosmological information hidden in the structure & dynamics of the Cosmic Web ?
 - How to extract such information, given the large variety and differences between methods to dissect the Cosmic Web
- Galaxies
 - How are galaxies influenced by the weblike nature of the cosmic mass distribution in which they form & evolve ?
- Patterns:
 - What is a filament ?
 - What is a wall ?
 - What is a void ?
- Reconstruction:
 - How to map the cosmic mass distribution such that its weblike & multiscale nature is retained ?